

Design of AC-DC PFC High-Order Converters with Regulated Output Current for Low Power Applications

M. Bodetto, *Student Member, IEEE*, A. El Aroudi, *Senior Member, IEEE*, A. Cid-Pastor *Member, IEEE*, J. Calvente *Member, IEEE*, and Luis Martínez-Salamero, *Senior Member, IEEE*.

Abstract - AC-DC PFC circuits used in low power applications have to overcome important power quality problems related to crest and power factors as well as total harmonic distortion, and in many cases they have to exhibit a high degree of output regulation. The design of efficient drivers for low power applications using high-order converters is considered in this paper. Power factor correction is achieved by imposing a loss-free resistor behaviour to SEPIC and Ćuk converters by means of an internal loop based on sliding-mode control, which requires a hysteretic comparator for its implementation. However, with a constant hysteresis width, the system exhibits harmful harmonic distortion in the input line current waveform, so that a variable hysteresis window is used instead to avoid this distortion near the zero crossings of the input current. The subsequent analysis of the ideal sliding dynamics around the equilibrium point allows the design of an outer control loop to regulate the output current. Mathematical analysis, numerical simulations and experimental results are presented to demonstrate the functionality of the proposed technique obtaining a significant improvement in terms of decreasing the total harmonic distortion. A dimmable LEDs driver supplying an HBLEDs string with a wide range of output current regulation illustrates the design.

Index Terms —HBLEDs, power factor corrector (PFC), loss-free resistor (LFR), sliding-mode control (SMC), Hysteresis modulation (HM).

I. INTRODUCTION

Power factor corrector (PFC) design is focused in obtaining high power factor (PF), and low total harmonic distortion (THD). This aim is extended to industrial, commercial and residential scenarios where a large number of electronic devices with this PF issues are used. In this sense, high power quality is increasingly required for power supply systems in order to fulfill the international standards such as IEEE Std. 519, IEC 61000-3-2 or EN 61000-3-2 [1, 2]. For this purpose, and specially in low power applications, switched-mode AC-DC PFC circuits are designed in order to ensure a high PF [3-5]. In this case, some harmonics pollution in current/voltage are

still observed due to the switching effects and/or the zero crossing distortion.

The aim of an active PFC circuit is to obtain a resistive behaviour to the circuit input port. This stage can be easily implemented with a diode bridge and with DC-DC converter stages (Fig. 1a). On the other hand, in most low power applications the DC voltage required is lower than the sinusoidal peak, and exceeds tens of volts. Hence, this DC-DC stage should have the ability to step-up and step-down the input voltage in order to raise or reduce the rectified voltage to obtain the appropriate DC voltage value (Fig. 1b).

Input power quality and output voltage regulation can be improved employing indistinctly two or more stages, which eventually result in a fast dynamic response [6]. On the contrary, single stage PFC circuits are less popular due to its difficult output regulation. Although, one converter for PFC and another stage for controlling the output variables it is generally preferred, it is expected that the use of one conversion stage combining both features will improve the efficiency at the expense of making the design more complex.

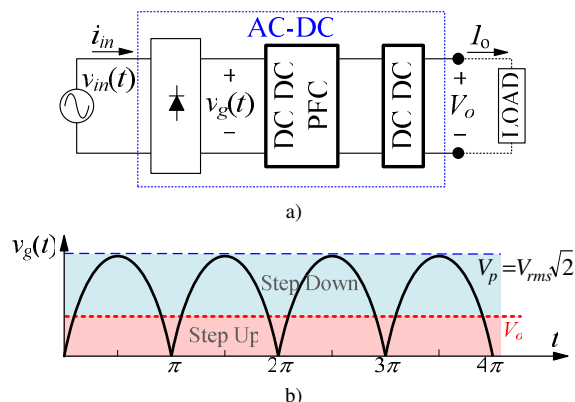


Fig. 1 a) General scheme of PFC circuit, b) waveform of DC-DC stage input voltage and output voltage V_o .

High order topologies refer to voltage step-up and step-down combinations, in which the most suitable for PFC are the Ćuk and SEPIC converters [7]. These converters, under pulse width modulation operation (PWM) and working in discontinuous conduction mode (DCM), exhibit resistive input impedance [4, 8, 9] and therefore can be used as PFC circuits. However, the existence of both pulsating input currents and DCM mode impose the insertion of an EMI input filter to fulfil harmonic standards. This is also the case of the topologies described in [10, 11] employing different control methods. In [12], the SEPIC converter without EMI filter has been proposed to work as a high efficiency adaptation single power stage with active PFC. The PFC has been carried out by means of a Sliding-Mode Control (SMC) forcing the converter to behave as a

Manuscript received ———; revised ———; accepted ———. Date of publication ———; date of current version ———. This work was partially supported by the Spanish Ministerio de Educación e Innovación under grants DPI2013-47437-R, DPI2013-47293-R and CSD2009-00046.

The authors are with the Departament d'Enginyeria Electrònica, Elèctrica i Automàtica, Escola Tècnica Superior d'Enginyeria, Universitat Rovira i Virgili, 43007, Tarragona, Spain (<http://deeea.urv.cat/gaei/index.php> e-mails: {mirkobodetto, angelcid, abdelali.elaroudi, javier.calvente, luis.martinez}@urv.cat, mirkobodetto@hotmail.com).

Copyright (c) 2013 IEEE. Personal use of this material is permitted. However, permission to use this material for any other purposes must be obtained from the IEEE by sending an email to pubs-permissions@ieee.org.

Colour versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Loss Free Resistor (LFR) [13], so that the converter input port behaves as a pure resistor and all the absorbed power by this resistor is transferred to the output port.

The synthesis of an LFR [14-16] can be carried out by imposing in steady-state the following relationship between the input variables

$$I_1 = g \cdot V_g \quad (1)$$

where I_1 , and V_g are the steady-state averaged values of the instantaneous input variables shown in Fig. 2, g represents the conductance characteristic of the PFC input port and is given by $g(t) = k_s \cdot G_{REF}(t)$; where k_s is the voltage sensor gain, and $G_{REF}(t)$ is a reference given by an external control loop regulating the converter output current.

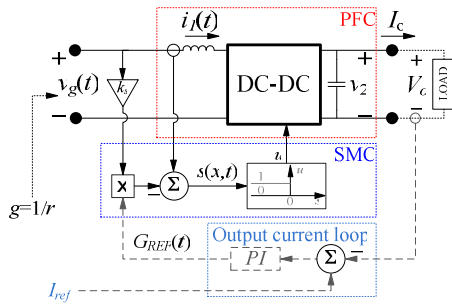


Fig. 2 Block diagram of a SMC-based LFR using a step-up/step-down DC-DC converter.

It has to be pointed out that imposing a sliding-mode regime to the input current requires $i_1(t)$ to be a continuous (non pulsating) function of time, this implying that $i_1(t)$ must be an inductor current what justifies the direct application of the method to both SEPIC and Ćuk converters. Also, note that SMC theory implies an infinite switching frequency that should be implemented by means of an ideal comparator as the one depicted in Fig. 2, whose output is given by $u=1$ when $s(x,t) < 0$, and $u=0$ when $s(x,t) > 0$.

However, the practical implementation of a SMC in switching converters requires a hysteresis comparator to limit the switching frequency to an acceptable range. The use of a constant hysteresis width results in a variable switching

frequency that depends on the input voltage value. This dependence provokes a loss of the sliding-mode regime and yields a very low value of the switching frequency near the zero crossings instants of the input voltage as illustrated in Fig. 3 in the case of SMC-based Ćuk converter [17].

To mitigate this problem two different techniques were proposed. The first one consists in a PI controller applied to the switching function $s(x,t)$ in order to increase the value of this signal either when the system fails to perform the switching action due to the loss of the sliding-mode regime or when it fails to reach the limits imposed by the hysteresis window [18]. Although an increase in the switching frequency near the zero crossing is obtained, another kind of distortion in the input current $i_1(t)$ waveform arises and therefore the PF and input current THD (I-THD) are negatively affected as it can be deduced observing Fig. 4.

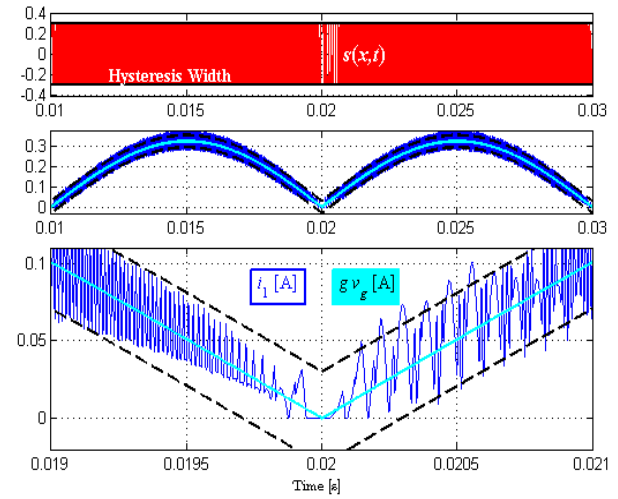


Fig. 4 Input current distortion in SMC when adding a PI controller to the switching surface.

The second technique consists in a time-varying hysteresis width which is made enough small when the input voltage approaches zero. Hence, narrowing the hysteresis width cancels the negative effect of the small value of the input voltage and results in an increase of the switching frequency rather than in

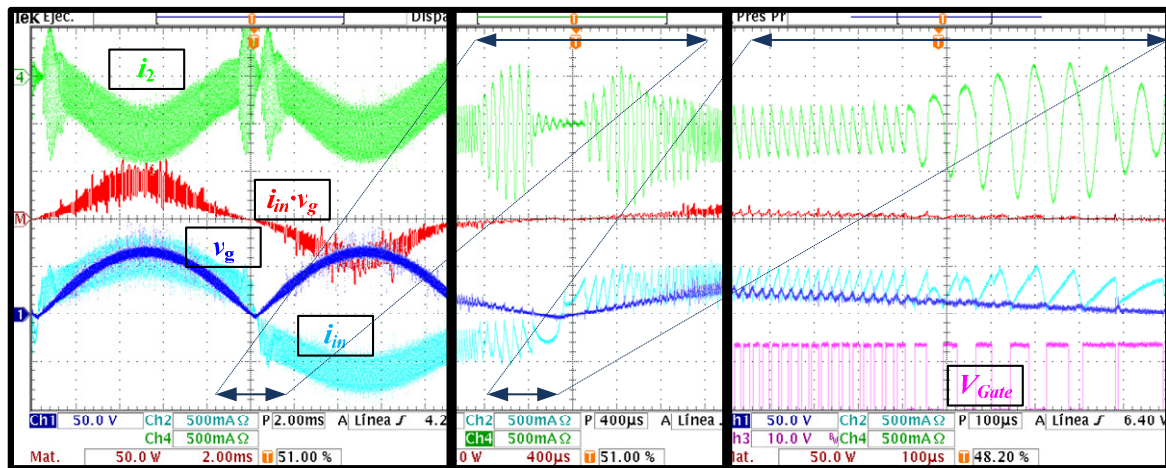


Fig. 3 Loss of sliding-mode regime of an LFR based on the Ćuk converter near the zero crossing of the inductor current.

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

3

its decrease. Satisfactory preliminary results recently published in [19] are provided by this technique, which is now exhaustingly covered in this paper in the design of a voltage step-up/step-down converter with non-pulsating input current.

Hence, the aim of the study here reported is to present an holistic design of a single stage voltage step-up/ step-down low power AC-DC PFC converter having both a low input current THD and a wide range output current regulation. The dynamic analysis of Ćuk and SEPIC converters includes the synthesis of the SM-based LFR, the study of the ideal sliding dynamics (ISD) around the equilibrium point and the design of an external control loop to regulate the output current. This paper provides a theoretical basis for the dynamic analysis together with clear guidelines for the control implementation. As an example, the proposed approach will be applied to the design of an HBLED power supply in which the nominal operating output voltage is lower than the input line voltage. Since the luminous flux and the HBLEDs current are proportional, the output current error with respect to a reference is processed by means of a PI controller in order to regulate the HBLEDs luminous flux.

The remains of the paper is organized as follows. The synthesis of an ideal LFR for AC-DC PFC using Ćuk and SEPIC converters and the corresponding mathematical modelling are described in Section II, this revealing the unconditionally stable nature of the Ćuk converter. In section III, the variable hysteresis width design is presented and its experimental results in a Ćuk converter are compared with those of the constant width approach. The decrease of the total harmonic distortion is also illustrated in section III. The design of the outer control loop for output voltage regulation is covered in section IV. Finally, the conclusions are summarized in Section V.

II. SYNTHESIS OF IDEAL LFR FOR AC-DC PFC APPLICATIONS

In this section the mathematical description of the system acting as a LFR with an input voltage $v_g(t) = V_m |\sin(\omega t)|$ is reviewed [14] and adapted to the case of SEPIC and Ćuk converters supplying a serial string of n HBLEDs. The goal of this section is to provide a first assessment on the stability of both converters.

A. Mathematical Description

The LFR behaviour can be obtained using a DC-DC switching converter with a sliding-mode regulation loop whose switching surface is given by

$$s(x, t) = i_1 - g \cdot v_g(t) \quad (2)$$

where i_1 is the input current, $v_g(t)$ is the input voltage and $g = 1/r$ is the LFR emulated conductance, r being its emulated resistance. Under sliding-mode regime and in steady-state operation, $s(x, t) = 0$, and therefore $I_1 = g \cdot V_g$, so that (1) is satisfied. To simplify the design process, $g(t)$ is assumed first constant, i.e., $g(t) = k_s \cdot G_{REF}$, i.e., only the inner current loop will be considered as shown in Fig. 5a and Fig. 5b.

It can be observed in both figures that the output voltage can be expressed as $V_{LED} = V_F + I_o rd$, where $rd = n \cdot rd'$ and $V_F = n \cdot V_F'$, n being the number of HBLEDs in series, rd' the dynamic resistance and V_F' the forward voltage drop of a single LED respectively.

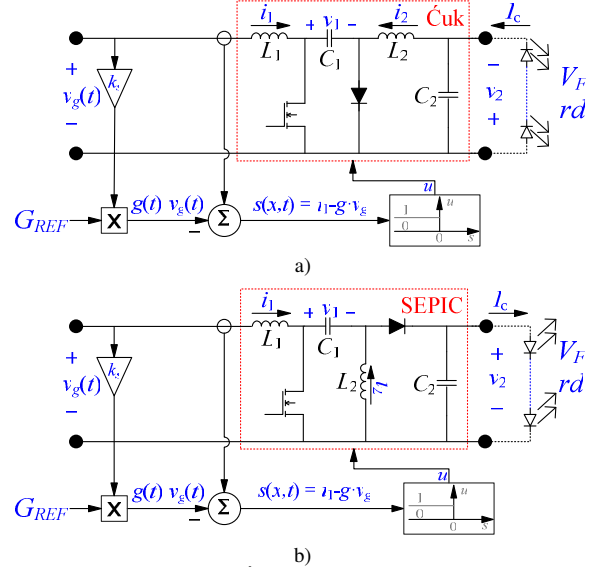


Fig. 5 Block diagram of a) Ćuk and b) SEPIC converters working as an LFR under SMC.

Assuming continuous conduction mode (CCM) operation implies that the system switches between two different topologies corresponding to the two states of the MOSFET, namely, ON ($u(t)=1$) or OFF ($u(t)=0$). The system state equations are therefore expressed as follows

$$\begin{aligned} \dot{x}(t) &= A_1 \cdot x(t) + B_1 \quad \text{for } u = 1 \\ \dot{x}(t) &= A_2 \cdot x(t) + B_2 \quad \text{for } u = 0 \end{aligned} \quad (3)$$

where $x(t) = [i_1(t) \ i_2(t) \ v_1(t) \ v_2(t)]^T$ is the vector of the state variables for both DC-DC converters and the over dot stands for derivation with respect to time. The matrices A_i , and vectors B_i (with $i = 1, 2$) are state matrices and input vectors in each topology of the converter. These matrices are depicted in TABLE I for each converter.

Equations (3) can be combined into a single bilinear expression given by

$$\dot{x}(t) = [A_1 \cdot x(t) + B_1]u + [A_2 \cdot x(t) + B_2](1-u) \quad (4)$$

which can be expressed as follows:

$$\dot{x}(t) = A_2 \cdot x(t) + B_2 + [(A_1 - A_2) \cdot x(t) + (B_1 - B_2)]u \quad (5)$$

Defining $A = A_2$, $\delta = B_2$, $B = A_1 - A_2$, $\gamma = B_1 - B_2$, the following bilinear model is obtained

$$\begin{aligned} \dot{x}(t) &= f(x, t) + g(x, t) \cdot u \quad \text{where } f(x, t) = A \cdot x(t) + \delta, \text{ and} \\ g(x, t) &= B \cdot x(t) + \gamma \end{aligned} \quad (6)$$

TABLE I STATE MATRICES AND INPUT VECTORS IN EACH TOPOLOGY, TC, EQUIVALENT CONTROL, AND EXISTENCE CONDITIONS OF SMC FOR BOTH CONVERTERS.

	A_1	$A_2 = A$	$B_1=B_2=\delta, (\gamma=0)$	$B = A_1 - A_2$	TC	$u_{eq}(t)$ $\alpha = 1 - \frac{g \cdot L_1 \omega}{\tan(\omega t)}$	Existence conditions of SMC
$\dot{C}uk$	$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{L_2} & \frac{-1}{L_2} \\ 0 & \frac{-1}{C_1} & 0 & 0 \\ 0 & \frac{1}{C_2} & 0 & \frac{-1}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} 0 & 0 & \frac{-1}{L_1} & 0 \\ 0 & 0 & 0 & \frac{-1}{L_2} \\ \frac{1}{C_1} & 0 & 0 & 0 \\ 0 & \frac{1}{C_2} & 0 & \frac{-1}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} \frac{v_g(t)}{L_1} \\ 0 \\ 0 \\ \frac{V_F}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} 0 & 0 & \frac{1}{L_1} & 0 \\ 0 & 0 & \frac{1}{L_2} & 0 \\ \frac{-1}{C_1} & \frac{-1}{C_1} & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$	$\frac{v_1}{L_1} \neq 0$	$1 - \frac{v_g}{v_1} \alpha$	$0 < v_g < v_1 / \alpha$
SEPIC	$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{L_2} & 0 \\ 0 & \frac{-1}{C_1} & 0 & 0 \\ 0 & 0 & 0 & \frac{-1}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} 0 & 0 & \frac{-1}{L_1} & \frac{-1}{L_1} \\ 0 & 0 & 0 & \frac{-1}{L_2} \\ \frac{1}{C_1} & 0 & 0 & 0 \\ \frac{1}{C_2} & \frac{1}{C_2} & 0 & \frac{-1}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} \frac{v_g(t)}{L_1} \\ 0 \\ 0 \\ \frac{V_F}{r_d C_2} \end{bmatrix}$	$\begin{bmatrix} 0 & 0 & \frac{1}{L_1} & \frac{1}{L_1} \\ 0 & 0 & \frac{1}{L_2} & \frac{1}{L_2} \\ \frac{-1}{C_1} & \frac{-1}{C_1} & 0 & 0 \\ \frac{-1}{C_2} & \frac{-1}{C_2} & 0 & 0 \end{bmatrix}$	$\frac{v_1 + v_2}{L_1} \neq 0$	$1 - \frac{v_g}{v_1 + v_2} \alpha$	$0 < v_g < (v_1 + v_2) / \alpha$

B. Equivalent Control

Taking into account (6), the time derivative of the switching surface can be expressed as follows:

$$\begin{aligned} \dot{s}(x, t) &= \frac{\partial s}{\partial x} \dot{x} - (g \cdot \dot{v}_g(t) + \dot{g} \cdot v_g(t)) \\ &= \langle \nabla s, [f(x, t) + g(x, t)u] \rangle - (g \cdot \dot{v}_g(t) + \dot{g} \cdot v_g(t)) \end{aligned} \quad (7)$$

where the notation $\langle a, b \rangle$ denotes the scalar product of a and b , and ∇ stands for the gradient operator. According to the equivalent control method [20-22], a necessary condition for the existence of a sliding motion on the switching surface is given by the transversality condition (TC).

$$\langle \nabla s, g(x, t) \rangle \neq 0 \quad (8)$$

Considering the gradient of the switching surface under study (2), and given that $\gamma = 0$ for both converters, the TC (8) is clearly fulfilled (TABLE I), and a sliding-mode can exist. Imposing the condition $\dot{s}(x, t)|_{u=u_{eq}} = 0$ leads to the following expression of the equivalent control:

$$u_{eq}(t) = \frac{(g \cdot \dot{v}_g(t) + \dot{g} \cdot v_g(t)) - \langle \nabla s, f(x, t) \rangle}{\langle \nabla s, g(x, t) \rangle} \quad (9)$$

In the equivalent control method, the discontinuous variable u is substituted by a continuous variable $u_{eq}(t)$ in (5), this representing the control law that constrains the state trajectories on the switching surface defined by $s(x, t) = 0$. This equivalent control is limited by the maximum and minimum values of the discontinuous variable u , i.e.,

$$0 < u_{eq}(t) < 1 \quad (10)$$

Also, substituting the expression of u_{eq} in (10) leads to the sliding-mode existence conditions, which are listed in TABLE I, where it can be also observed that an auxiliary parameter α has been defined as

$$\alpha = 1 - \frac{g L_1 \omega}{\tan(\omega t)} \quad (11)$$

After some algebra, it can be seen that this parameter is practically equal to one except for a small discontinuity in a zero crossing point. Although a loss of sliding regime is temporarily caused by this discontinuity, the system recovers the sliding regime after this instant, so that this effect is neglected in the rest of the analysis. Moreover, the simplification mentioned before, i.e., $g(t)$ is constant implies $\dot{g} = 0$.

C. Quasi-Static Approach

To simplify the analysis, a quasi-static approach is used [10, 23-25]. The line frequency (50 or 60 Hz) is significantly below the switching frequency, hence, the input voltage of the DC-DC converters can be considered constant during few consecutive switching periods. Thus, this input voltage and consequently the corresponding equilibrium point will be parameterized as a function of $\theta = \omega \cdot t$. Therefore, the full range values of $v_g(\theta)$ will be obtained for $\theta = (0, \pi/2)$.

D. Ideal Sliding Dynamics

The ISD model is represented by a set of nonlinear differential equations by substituting in (6) the discontinuous control u by the continuous variable u_{eq} given in (9) and taking into account the constraint (2) imposed by the switching condition (i.e. $i_1 = g \cdot v_g$). The model for both converters is shown in TABLE II where it can be observed an order reduction in the system dynamics due to the SMC action.

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

5

TABLE II IDEAL SLIDING DYNAMICS.

	Ćuk	SEPIC
$\dot{x} = \begin{bmatrix} f_1(x) \\ f_2(x) \\ f_3(x) \end{bmatrix} := \begin{bmatrix} \dot{i}_1 \\ \dot{v}_1 \\ \dot{v}_2 \end{bmatrix}$	$\begin{bmatrix} \frac{-v_2 + v_1 - v_g(\theta)}{L_2} \\ \frac{(v_g(\theta) - v_1)i_2 + g \cdot v_g^2(\theta)}{v_1 \cdot C_1} \\ \frac{i_2 \cdot r_d - v_2 + V_F}{r_d \cdot C_2} \end{bmatrix}$	$\begin{bmatrix} \frac{v_1 - v_g(\theta)}{L_2} \\ \frac{(v_g(\theta) - v_1 - v_2)i_2 + g \cdot v_g^2(\theta)}{(v_1 + v_2) \cdot C_1} \\ \frac{-v_2^2 + (V_F - v_1) \cdot v_2 + v_g(\theta)(g \cdot v_g(\theta) + i_2) \cdot r_d + v_1 \cdot V_F}{(v_1 + v_2) \cdot r_d \cdot C_2} \end{bmatrix}$

Based on the ISD equations the equivalent circuits of both Ćuk and SEPIC switching converters are shown in Fig. 6.

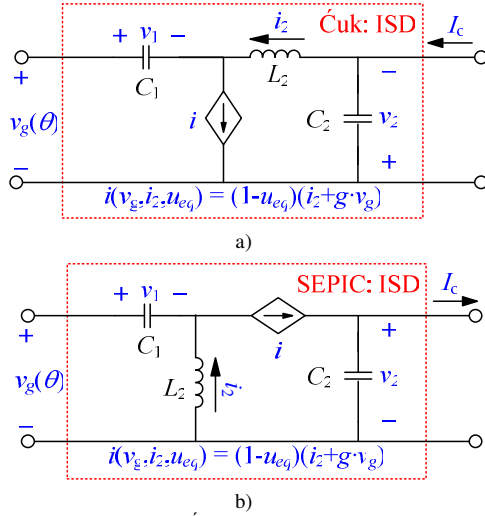


Fig. 6 ISD model of a) Ćuk converter and b) SEPIC converter.

The coordinates of the equilibrium point of the ISD is given by:

$$X_{ss}(\theta) = \begin{bmatrix} g \cdot v_g(\theta) \\ g \cdot v_g^2(\theta)/V_2(\theta) \\ v_g(\theta) + V_2(\theta) \\ V_2(\theta) \end{bmatrix}_{\text{Ćuk}} = \begin{bmatrix} g \cdot v_g(\theta) \\ g \cdot v_g^2(\theta)/V_2(\theta) \\ v_g(\theta) \\ V_2(\theta) \end{bmatrix}_{\text{SEPIC}} \quad (12)$$

$$\text{where } V_2(\theta) = \frac{1}{2} \left(V_F + \sqrt{V_F^2 + 4g \cdot v_g^2(\theta)r_d} \right)$$

According to the expressions of u_{eq} listed in TABLE I, the corresponding equivalent control for both equilibrium points given by (12) can be expressed as follows

$$u_{eq}(\theta) = 1 - \frac{v_g(\theta)}{v_g(\theta) + V_2(\theta)} \alpha$$

Fig. 7 shows the plot of the expression in (13). Its corresponding numerical simulation using the switched model is also given in the same figure where a remarkable agreement between the ISD and the original switching system can be observed.

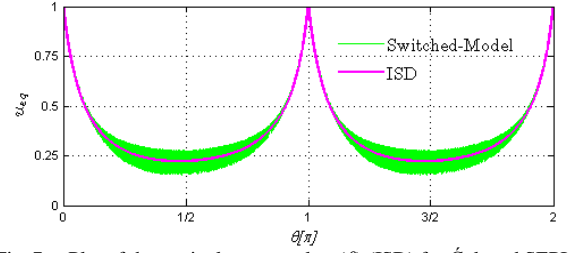


Fig. 7 Plot of the equivalent control $u_{eq}(\theta)$ (ISD) for Ćuk and SEPIC switching converters, in comparison with the actual value of u (switched-model).

E. Stability Analysis

Taking into account the ISD equations given in TABLE II, a linearization around the equilibrium point $X_{ss}(\theta)$ is now carried out in order to study the converter stability. The corresponding Jacobian matrix $J(\theta)$ can be expressed as follows

$$J(\theta) = \begin{bmatrix} \frac{\partial f_1(x)}{\partial i_2} & \frac{\partial f_1(x)}{\partial v_1} & \frac{\partial f_1(x)}{\partial v_2} \\ \frac{\partial f_2(x)}{\partial i_2} & \frac{\partial f_2(x)}{\partial v_1} & \frac{\partial f_2(x)}{\partial v_2} \\ \frac{\partial f_3(x)}{\partial i_2} & \frac{\partial f_3(x)}{\partial v_1} & \frac{\partial f_3(x)}{\partial v_2} \end{bmatrix}_{X_{ss}(\theta)} \quad (14)$$

Therefore, the corresponding 3rd order characteristic polynomial is given by

$$\det(J - sI) = a_3(\theta)s^3 + a_2(\theta)s^2 + a_1(\theta)s + a_0(\theta) \quad (15)$$

where I is the identity matrix, and parameters $a_i(\theta)$ of each converter are listed in TABLE III.

By applying the Routh-Hurwitz (RH) criteria to the characteristic polynomial of each converter, the corresponding stability conditions are obtained and shown in TABLE III, where it can be observed that the stability is ensured for the whole range of $v_g(\theta)$ in the Ćuk converter. However, the stability is guaranteed in a SEPIC converter provided that the condition presented in TABLE III is fulfilled [14]. For that reason, a Ćuk converter prototype will be used in the sequel to verify the theoretical predictions.

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

6

TABLE III COEFFICIENTS OF THE CHARACTERISTIC EQUATION AND STABILITY CONDITIONS.

	Cuk	SEPIC
	$a_3(\theta) = 1$	$a_3(\theta) = 1$
	$a_2(\theta) = \frac{C_1(v_g(\theta) + V_2(\theta)) \cdot V_2(\theta) + g \cdot v_g^2(\theta) \cdot r_d \cdot C_2}{C_1 \cdot C_2 (v_g(\theta) + V_2(\theta)) r_d \cdot V_2(\theta)}$	$a_2(\theta) = \frac{C_1(v_g(\theta) + V_2(\theta)) \cdot V_2(\theta) + g \cdot v_g^2(\theta) \cdot r_d \cdot (C_1 + C_2)}{C_1 \cdot C_2 (v_g(\theta) + V_2(\theta)) r_d \cdot V_2(\theta)}$
	$a_1(\theta) = \frac{r_d[(C_1 + C_2) \cdot V_2^2(\theta) + C_1 \cdot V_2(\theta) \cdot v_g(\theta)] / L_2 + g \cdot v_g^2(\theta)}{C_1 \cdot C_2 (V_2(\theta) + v_g(\theta)) r_d \cdot V_2(\theta)}$	$a_1(\theta) = \frac{r_d \cdot C_2 \cdot V_2^2(\theta) / L_2 + g \cdot v_g^2(\theta)}{C_1 \cdot C_2 (V_2(\theta) + v_g(\theta)) r_d \cdot V_2(\theta)}$
	$a_0(\theta) = \frac{(r_d \cdot g \cdot v_g^2(\theta) + V_2^2(\theta)) / L_2}{C_1 \cdot C_2 (v_g(\theta) + V_2(\theta)) r_d \cdot V_2(\theta)}$	$a_0(\theta) = \frac{(r_d \cdot g \cdot v_g^2(\theta) + V_2^2(\theta)) / L_2}{C_1 \cdot C_2 (v_g(\theta) + V_2(\theta)) r_d \cdot V_2(\theta)}$
R-H criteria: necessary condition	$a_i(\theta) > 0 \quad i = 0 \dots 3$	
R-H criteria: sufficient conditions	$(a_2(\theta) \cdot a_1(\theta) - a_0(\theta)) > 0$	
Stability conditions	Unconditionally stable	$V_1(\theta) / V_2(\theta) < C_2 / C_1$

III. VARIABLE HYSTERESIS WIDTH

A. Operating Switching Frequency

Assuming quasi-static steady-state operation in SMC allows describing the waveforms of the control signal $s(x,t)$ as triangular signals as depicted in Fig. 8 where the switching frequency f_o is given by [26]

$$f_o = \frac{1}{T} = \frac{1}{t_{on} + t_{off}} = \frac{1}{2\Delta} \frac{m_{on} \cdot m_{off}}{m_{on} + m_{off}}$$

where t_{on} and t_{off} are the interval duration for $u = 1$ and $u = 0$ respectively, $T = t_{on} + t_{off}$, m_{on} and m_{off} are the slopes of the control signal $s(x,t)$, and Δ is the constant hysteresis width. The respective expressions of m_{on} and m_{off} slopes are given by

$$\begin{aligned} m_{on} &= \nabla s(x) \cdot \dot{x} \Big|_{u=1} \\ m_{off} &= -\nabla s(x) \cdot \dot{x} \Big|_{u=0} \end{aligned} \quad (17)$$

and are listed in TABLE IV for both converters.

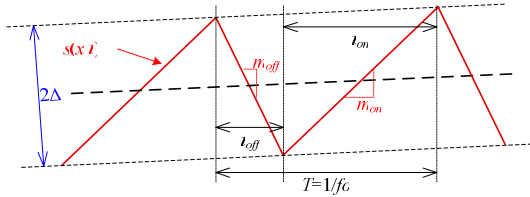


Fig. 8 Sliding surface in CCM steady-state operation determining the switching frequency (f_o).

TABLE IV SLOPES OF THE CONTROL SIGNAL AND SWITCHING FREQUENCY.

	Cuk	SEPIC
$m_{on}(\theta)$	$v_g(\theta) / L_1$	$v_g(\theta) / L_1$
$m_{off}(\theta)$	$(V_1(\theta) - v_g(\theta)) / L_1$	$(V_1(\theta) + V_2(\theta) - v_g(\theta)) / L_1$
$f_o(\theta)$	$\frac{1}{2\Delta L_1} \frac{v_g(\theta)(V_1(\theta) - v_g(\theta))}{V_1(\theta)}$	$\frac{1}{2\Delta L_1} \frac{v_g(\theta)(V_1(\theta) + V_2(\theta) - v_g(\theta))}{V_1(\theta) + V_2(\theta)}$

Besides, from the expression of the equilibrium point (12) and the insertion of (17) in (16), the switching frequency becomes

$$f_o(\theta) = \frac{1}{2\Delta L_1} \frac{V_2(\theta) \cdot v_g(\theta)}{(V_2(\theta) + v_g(\theta))} \quad (18)$$

Considering that the voltage $V_2(\theta)$ will be constant due to the regulation by an external control loop, it can be seen in (18) that the switching frequency has a maximum value at $v_g(\theta) = \pi/2 = V_m$ in the interval $0 < \theta < \pi/2$, and tends to zero if V_g tends to zero. Hence, for the parameters shown in TABLE V, the maximum switching frequency is: $f_o \approx 150$ kHz. Finally, the plot of $f_o(\theta)$ in a sliding-mode control implemented with constant hysteresis width is depicted in Fig. 9 for the full range of $v_g(\theta)$.

TABLE V DESIGN SPECIFICATIONS AND PARAMETER VALUES

Component	Value
Input Voltage	$v_g = 230$ V RMS / 230 V DC
9 x HBLED, Cree, Inc.	$V_f \approx 100$ V, $r_d \approx 30 \Omega$
“Xlamp MC-E” (Cool White)	$P_o = 45$ W, $I_{nom} = 350$ mA
L_1	9 mH
L_2	2 mH
C_1	40 nF
C_2	500 μF
$g = ks G$	$P_o = 45$ W, $g = P_o / V_{rms}^2 \approx 1/1000$
ks : Voltage sensor gain.	$ks = 1/5000$, $G_{REF} \approx 5$ S
Δ : Hysteresis width	$\Delta_i = 0.03$ A
S_I	IPP60R250CP
D	IDD04SG60C
Hysteresis modulation	AD633 (Analogue multiplier)
	TLE 2047 (AOx4)
SMC	AD633 (Analogue multiplier)
	LM319 (Comparator)
	CD4027 (FF RS)
	TC4427 (Driver)

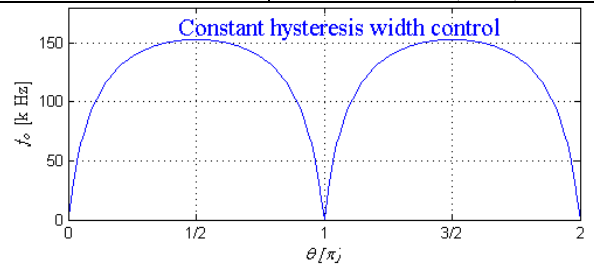


Fig. 9 Steady-state switching frequency (f_o) during one line cycle constant hysteresis width control (Δ).

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

7

B. Hysteresis Width Modulation

As it is shown in (18), the switching frequency increases when the hysteresis window (Δ) tends to zero. Therefore, to avoid a decrease of the switching frequency near the zero crossing, Δ is modulated so that it tends to zero when the input voltage does. The modulation applied to Δ is depicted in Fig. 10 and corresponds to the shape

$$\Delta(\theta) = \begin{cases} \delta \cdot v_g(\theta) & \text{if } \delta \cdot v_g(\theta) < \Delta_{i1} \\ \Delta_{i1} & \text{if } \delta \cdot v_g(\theta) > \Delta_{i1} \end{cases} \quad (19)$$

where $\delta = \Delta_{i1} \cdot k / V_m$; k is an amplifier gain, V_m is the input peak of the sinusoidal voltage. This amplifier is used only to vary the slope of width $\Delta(\theta)$ near the zero crossings. The evolution of the hysteresis width from zero to a maximum value Δ_{Max} can be observed in Fig. 11.

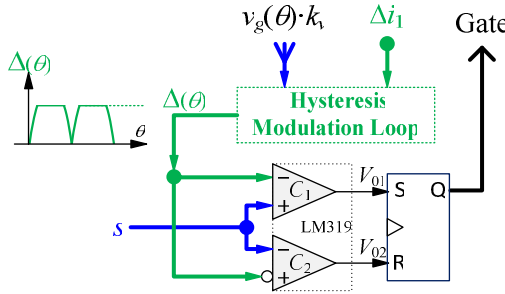


Fig. 10 Block diagram of hysteresis width modulation.

It can be seen from (18) that $\Delta(\theta)$ and the input voltage are proportional so they tend to zero in a similar way, this allowing an increase in the switching frequency near the zero-crossings and therefore a longer time in sliding-mode regime in this critical area.

The block diagram in Fig. 10 corresponds to (19). To ensure that $\Delta(\theta)$ is not greater than a pre-set value Δ_{i1} (Fig. 12a), a saturation block is used. Thus, when saturation takes place, the switching frequency is determined by (18) and when no saturation occurs (i.e.: in the zero crossings), the switching frequency near the zero crossing can be determined by substituting the modulated hysteresis width by $\Delta(\theta) = \delta \cdot v_g(\theta)$ in (18). Hence,

$$f_o(\theta) = \begin{cases} \frac{1}{2\delta \cdot L_1} \frac{V_2(\theta)}{(V_2(\theta) + v_g(\theta))} & \text{if } \alpha \cdot v_g(\theta) < \Delta_{i1} \\ \frac{1}{2\Delta_{i1} \cdot L_1} \frac{V_2(\theta) \cdot v_g(\theta)}{(V_2(\theta) + v_g(\theta))} & \text{if } \alpha \cdot v_g(\theta) > \Delta_{i1} \end{cases} \quad (20)$$

A plot of $f_o(\theta)$ for the conventional control based on constant hysteresis width and the control employing modulated hysteresis width is depicted in Fig. 12b. Compared to the constant hysteresis width situation, a significant increase in the switching frequency near the zero crossings can be observed. Thus, for the set of parameters of TABLE V, the maximum switching frequency occurs at $\theta = \pi$ yielding $f_o = V_m / (2 \cdot \Delta_{i1} \cdot L_1) \approx 600$ kHz, whereas the minimum switching frequency is the maximum switching frequency of the conventional control ($f_o \approx 150$ kHz). It should be noted that this frequency increase occurs at zero crossings of the input variables and therefore the switching losses are negligible and the overall switching frequency of the system will not be affected.

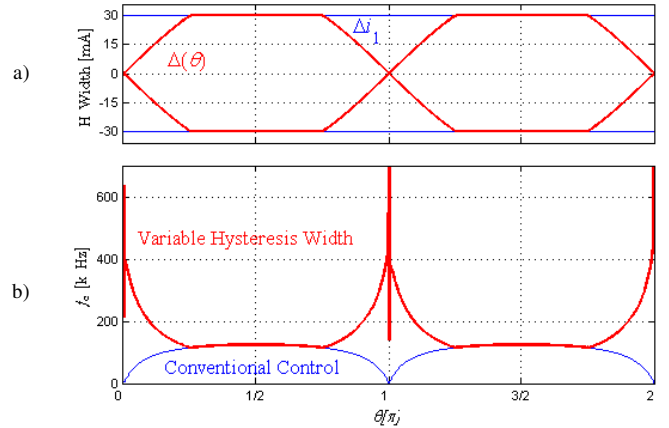


Fig. 12 a) Hysteresis width during one cycle with: conventional control (constant Δ), and with Δ tending to zero as v_g approaches zero. b) Steady-state switching frequency (f_o) during one line cycle with: conventional control (Δ), and with Δ tending to zero as v_g approaches zero.

C. Simulation and Experimental Design

With the aim of verifying the theoretical results concerning the stability of the system under SMC, time-domain numerical simulations have been carried out using PSIM simulation program [27]. The prototype has been designed to supply an

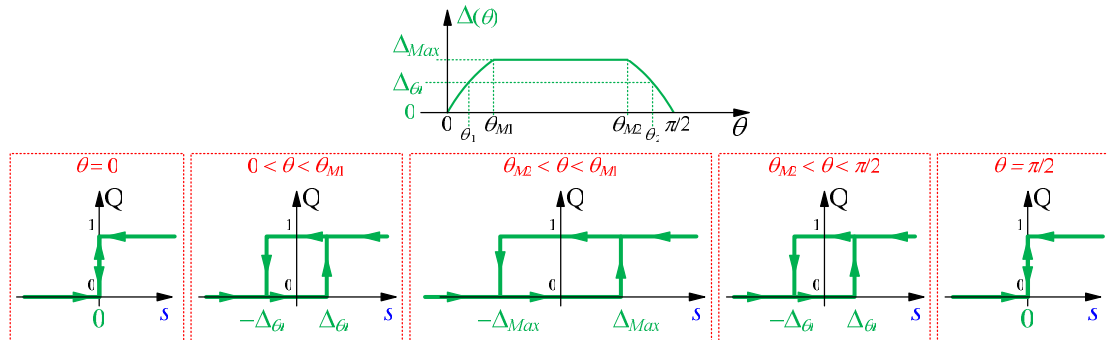


Fig. 11 Hysteresis width modulation as a function of signal $\Delta(\theta)$.

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

8

string of 9 HBLEDs “Xlamp MC-E” (Cool White) of Cree, Inc. The requirements regarding voltage and current for these diodes are typically from 200 to 700 mA and from 2.5 Vdc to 4 Vdc respectively (with a typical voltage forward of 3.2 V at 350 mA) [28]. The nominal values for both numerical simulations and prototyping are a DC input voltage $V_g = 230$ V and rated output power $P_o = 45$ W, corresponding to a serial string of 9 HBLEDs, or equivalently $V_{LED} = 100$ V. The switching frequency employed is 150 kHz, which ensures that the sliding regime is not lost for the previous values of input and output voltages. Reactive components have been selected assuming a certain degree of ripple in the state variables (between 10% and 20% of the mean value for each variable). All the converter parameters are shown in TABLE V.

In order to generate the switching signal $u(t)$, a hysteretic comparator with an analogue multiplier and a variable hysteresis window is used as depicted in Fig. 13b in a clear-cut contrast with the conventional approach of constant hysteresis width illustrated in Fig. 13a.

The system behaviour using a conventional control or variable hysteresis window is simulated in Fig. 14a and Fig. 14b respectively in the case of the Ćuk converter. It can be seen that the variable hysteresis width tends to zero as v_g approaches zero, thereby narrowing the width $\Delta(t)$ which implies an

increase in the switching frequency. Thus, the duty cycle is controlled down to very low values and a “clean” zero crossing is obtained. Also, when the system is controlled by a variable hysteresis window, the input current ripple is decreased near the zero crossings due to the decrease of the hysteresis width in this region. As a result, the converter behaves as an almost ideal LFR.

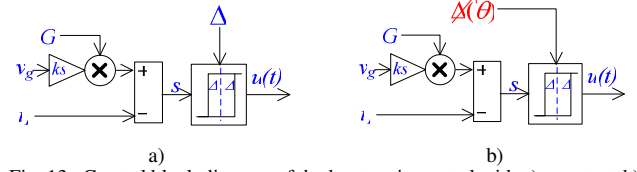


Fig. 13 Control block diagram of the hysteresis control with a) constant, b) variable hysteresis width.

Fig. 14 also shows the sum of both inductor currents ($i_1 + i_2$), which is zero near the zero crossings because the system enters temporarily into DCM. Moreover, in spite of the variable hysteresis width, Fig. 14b shows an oscillation of this sum near the zero crossings region that induces a temporary loss of the sliding regime until the system reaches again a quasi-static steady-state operation. It can be also shown by simulation that although the improvement in the PF is negligible (an increase

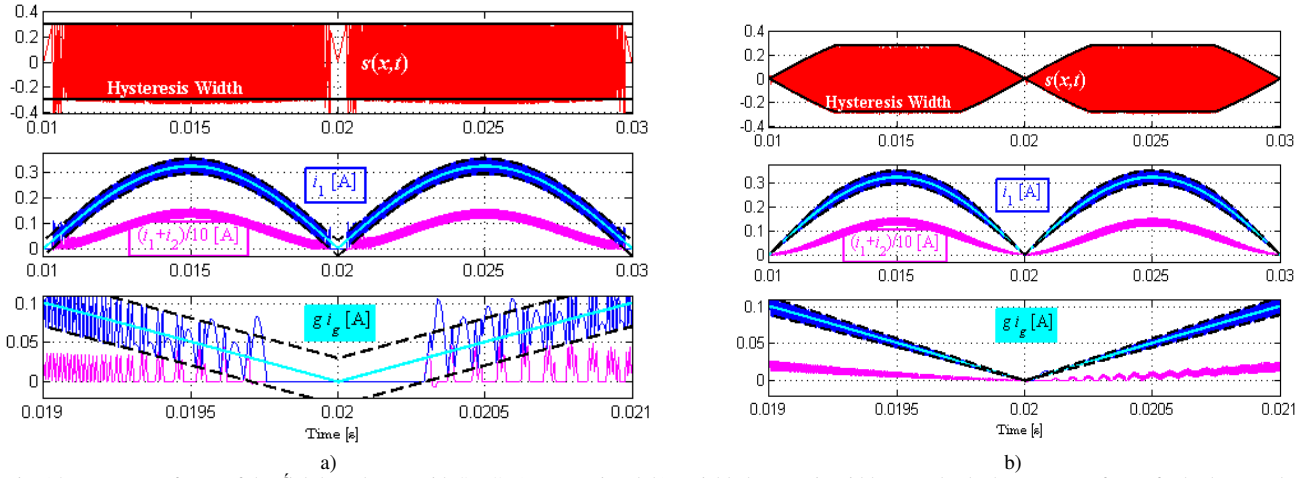


Fig. 14 Input waveforms of the Ćuk-based LFR with SMC: a) conventional, b) variable hysteresis width control. The bottom waveforms for both controls are a zoom of the intermediate plots.

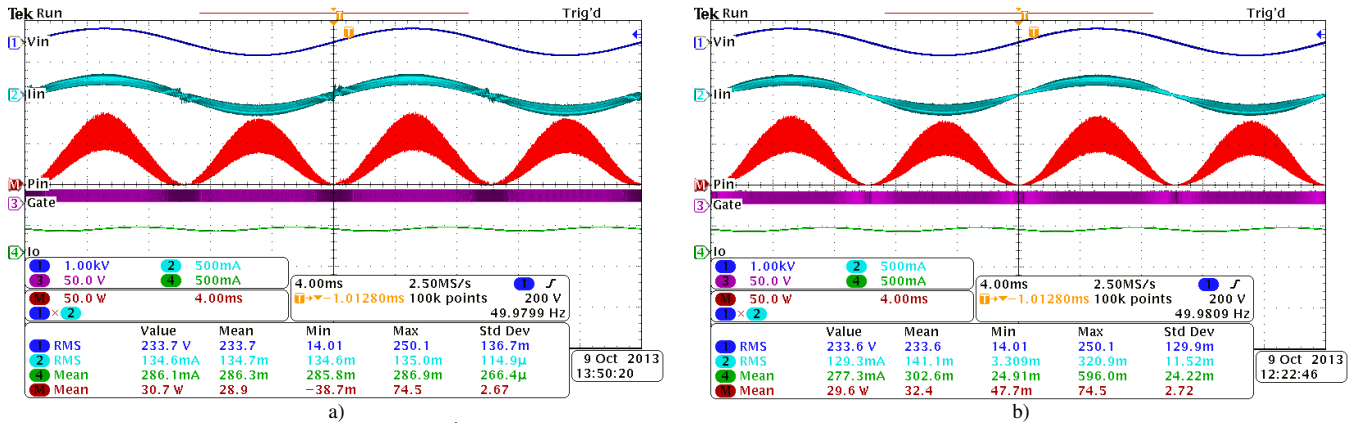


Fig. 15 Comparative waveforms of a Ćuk converter operating in SMC as LFR: a) convectional control, b) variable hysteresis width.

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) <

9

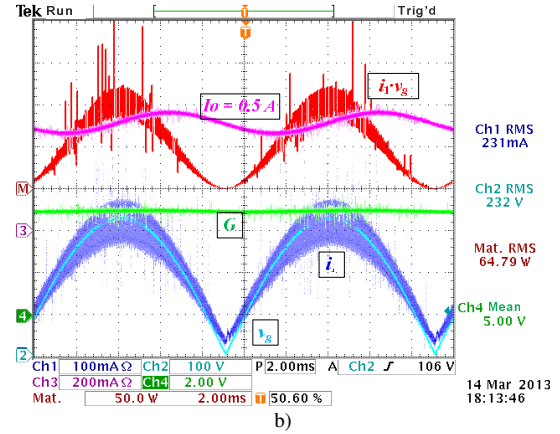
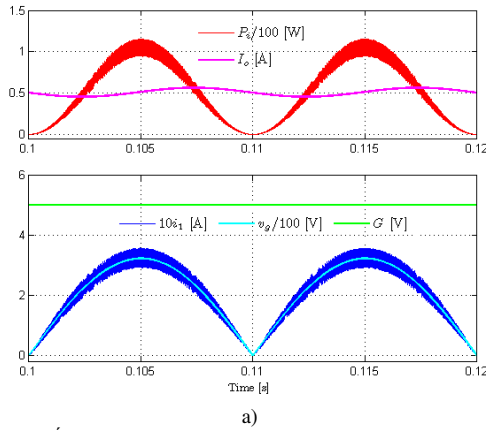


Fig. 16 Ćuk-based LFR converter controlled by SMC with a variable hysteresis width ($g=G/5000$ S): a) simulation, and b) experimental results.

of 0.19% over 99%), an important decrease of 2.5% of the I-THD is achieved, i.e., from 8.8% in the conventional control to 6.3% in the variable hysteresis width.

Fig. 15 corroborates the expected improvement of the variable hysteresis width control by showing the experimental results in a Ćuk-based LFR with SMC using conventional approach (Fig. 15a) and the proposed control (Fig. 15b)

Fig. 16a and Fig. 16b show respectively the simulated and experimental waveforms of the input voltage (v_g), input current (i_g), input power (p_g) and output current (I_o) for the Ćuk converter acting as LFR by means of an internal sliding-mode control loop. In both figures a perfect proportionality between input current and input voltage can be observed, thus validating the active PFC behaviour. The input conductance g relating the input signals is represented by the constant signal G which is provided by the outer control loop. Variables in the simulation are presented with a scaling factor to be depicted in a single graph.

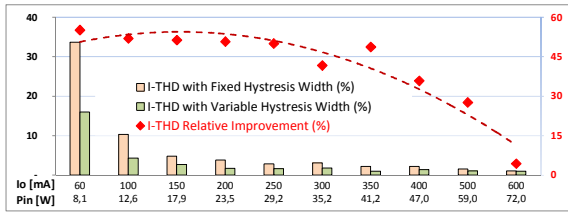


Fig. 17 I-THD for conventional control and variable hysteresis width respectively; and I-THD relative improvement vs. input power or Load current (Ćuk-based LFR converter).

D. THD Improvement

An extension of the analysis of the I-THD performed in the waveforms of Fig. 15a and Fig. 15b has been performed for different levels of load current (or input power). The corresponding results are depicted in Fig. 17, which illustrates the absolute values of I-THD for conventional control and for variable hysteresis width. Furthermore, the relative improvement for the last case is also shown. As an example, note that for the nominal load current of 350 mA the resulting I-THD is 40 % of that obtained with constant hysteresis width. This reduction in the harmonic contents is also obtained at lower power values as illustrated in Fig. 17.

Finally, power quality experimental results for each hysteresis type are plotted in Fig. 18 in the case of a load current of 60 mA (9 W input power). It can be observed (in red) that harmonics 3 and 9 for constant hysteresis width exceed the limit fixed by the harmonic standards IEC61000-3-2, class C (lighting equipment).

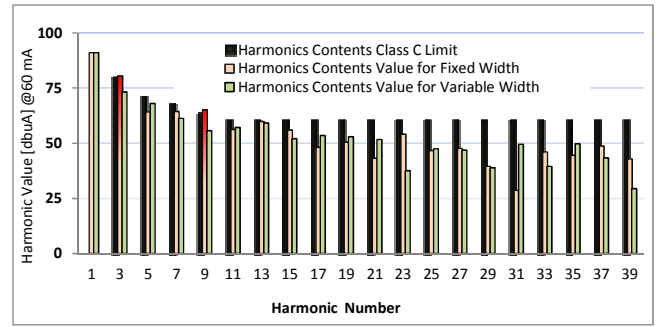


Fig. 18 Power quality experimental results: current harmonics contents for each hysteresis type, and standards IEC61000-3-2, class C (Ćuk-based LFR converter).

IV. OUTPUT CURRENT REGULATION DESIGN

A. Small-Signal Model

In order to design the outer control loop of the AC-DC PFC, a small-signal model (SSM) for both converters will be derived. From the non-linear ISD of TABLE II, it can be deduced that vector $\dot{x}$ can be expressed as follows

$$\dot{x} = f(x, p) \quad (21)$$

where x is the state vector and $p = [g \ v_g \ rd \ V_F]^T$ is the input and output disturbances vector.

In order to study the stability of the system, expression (20) will be linearized around the equilibrium point $X_{ss}(12)$. This linearization will be performed by extending the Jacobian matrix (14) corresponding to the state vector x to the disturbances vector p as follows

$$\dot{\hat{x}} = \left. \frac{\partial f(x, p)}{\partial x} \right|_{x_{ss}} \hat{x} + \left. \frac{\partial f(x, p)}{\partial p} \right|_{x_{ss}} \hat{p} \quad (22)$$

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) < 10

After some algebra, the output voltage $\hat{v}_2$ can be expressed in the complex domain s as a linear combination of the perturbations in the input voltage, LFR conductance, HBLED dynamic resistance and HBLED drop voltage, which results in the four transfer functions given in (22) whose parameters g_i , vg_i , rd_i , d_i for both converters are detailed in Annex I.

$$\begin{aligned} H_1(s) &= \left. \frac{\hat{v}_2(s)}{\hat{g}(s)} \right|_{\hat{v}_g=\hat{r}d=\hat{v}_F=0} = \frac{g_2 \cdot s^2 + g_1 \cdot s + g_0}{d_3 s^3 + d_2 s^2 + d_1 s + d_0} \\ H_2(s) &= \left. \frac{\hat{v}_2(s)}{\hat{v}_g(s)} \right|_{\hat{g}=\hat{r}d=\hat{v}_F=0} = \frac{vg_2 \cdot s^2 + vg_1 \cdot s + vg_0}{d_3 s^3 + d_2 s^2 + d_1 s + d_0} \\ H_3(s) &= \left. \frac{\hat{v}_2(s)}{\hat{r}d(s)} \right|_{\hat{g}=\hat{v}_g=\hat{v}_F=0} = \frac{rd_2 \cdot s^2 + rd_1 \cdot s + rd_0}{d_3 s^3 + d_2 s^2 + d_1 s + d_0} \\ H_4(s) &= \left. \frac{\hat{v}_2(s)}{\hat{v}_F(s)} \right|_{\hat{g}=\hat{v}_g=\hat{r}d=0} = \frac{vf_2 \cdot s^2 + vf_1 \cdot s + vf_0}{d_3 s^3 + d_2 s^2 + d_1 s + d_0} \end{aligned} \quad (23)$$

In order to regulate the load current, transfer function $H_1(s)$ should be considered since it represents the relation between output voltage v_2 (hence I_o) and control parameter G . The closed-loop dynamic model for both switching converters is shown in Fig. 19 where the effect of the inner loop is represented by H_1 and the output current regulation is carried out by the outer loop including a PI compensator.

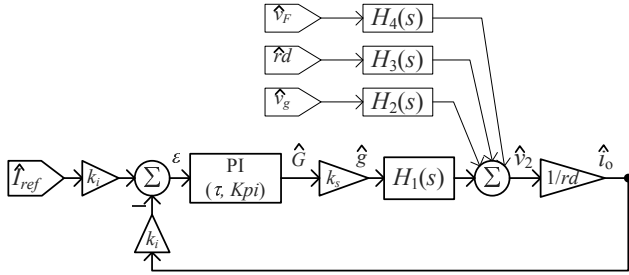


Fig. 19 Small-signal block diagram of Ćuk/SEPIC-based LFR with an outer loop for output current regulation.

It must be taken into account that when the output feedback bandwidth is increased, a ripple appears at twice the line frequency in the sensed variable (i_o) distorting the input parameter (G) and consequently the input current.

This distorted reference must be eliminated in order to obtain an undistorted input current. Thus, the bandwidth of the PI compensator must be relatively low to achieve a suitable response [29-31]. Hence, a compromise between bandwidth (speed response) and input current distortion has to be achieved. For light dimmer applications a slow response (100 ms) is appropriate. Using the Bode diagram depicted in Fig. 20 allows the selection of the PI compensator parameters as $\tau = 1/500$ s, $Kpi = 1/10$ for 66 degrees phase margin at a crossover frequency of 36 rad/s. The loop gain $T(s)$ has a zero at $s_z = -500$ rad/s and poles at $s_1 = -68.13$ rad/s, $s_{2,3} = (-1.67 \pm j 6.22) \cdot 10^4$ rad/s, besides a pole at the origin of the s -plane. This results in closed-loop poles located at, $s_{1,2-CL} = (-1.68 \pm j 6.28) \cdot 10^4$ rad/s, and $s_{3,4-CL} = (-36.8 \pm j 37.7)$ rad/s. It can be observed that the

latter are dominant and determine the dynamic response of the controlled converter with a damping coefficient of 0.7.

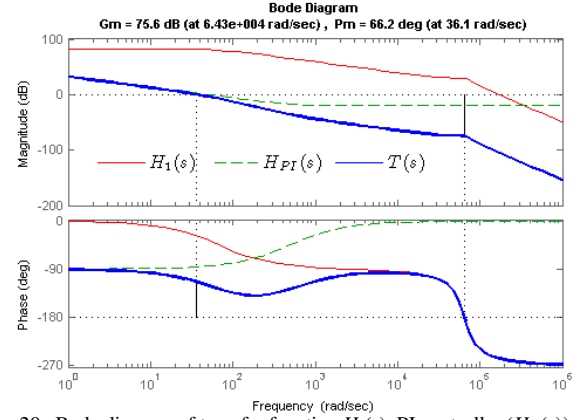


Fig. 20 Bode diagram of transfer function $H_1(s)$, PI controller ($H_{PI}(s)$), and loop gain $T(s)$ in the Ćuk converter-based LFR.

B. Practical Implementation

An experimental prototype has been developed to validate the theoretical analysis and PSIM simulations corresponding to the block diagram of the two-loop control circuit illustrated in Fig. 21, where the inner loop implements the PFC with variable hysteresis width and the external loop carries out the output current regulation of a string of 9 HBLEDs “Xlamp MC-E”. A detailed scheme of the control circuit is depicted in Fig. 22. Note that the proposed controller would be equivalent to the classical SMC if the output of the tracker (i) were directly connected to the inverter input (iv). Therefore, the added complexity with respect to SMC implementation is limited to the insertion of two operational amplifiers and an analogue multiplier.

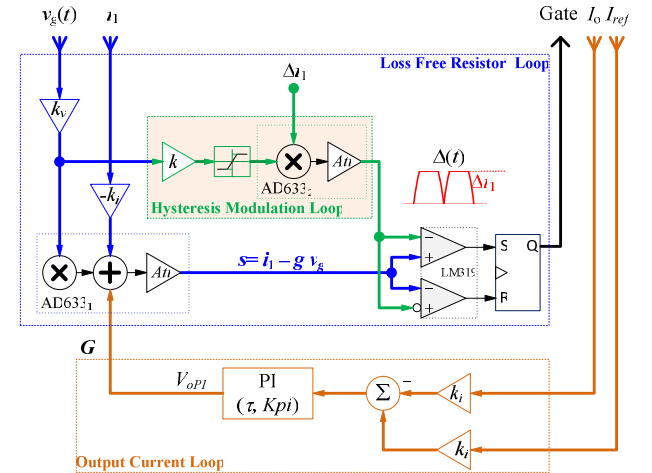


Fig. 21 Block diagram of the control stage Ćuk converter with two-loop control.

Since the use of hysteresis in the control circuit implies a variable switching frequency, this fact has been considered in the design of the magnetic components. Note that the practical operation range of the converter goes from 150 kHz to 400 kHz, and the ferrite cores of both inductors can operate

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) < 12

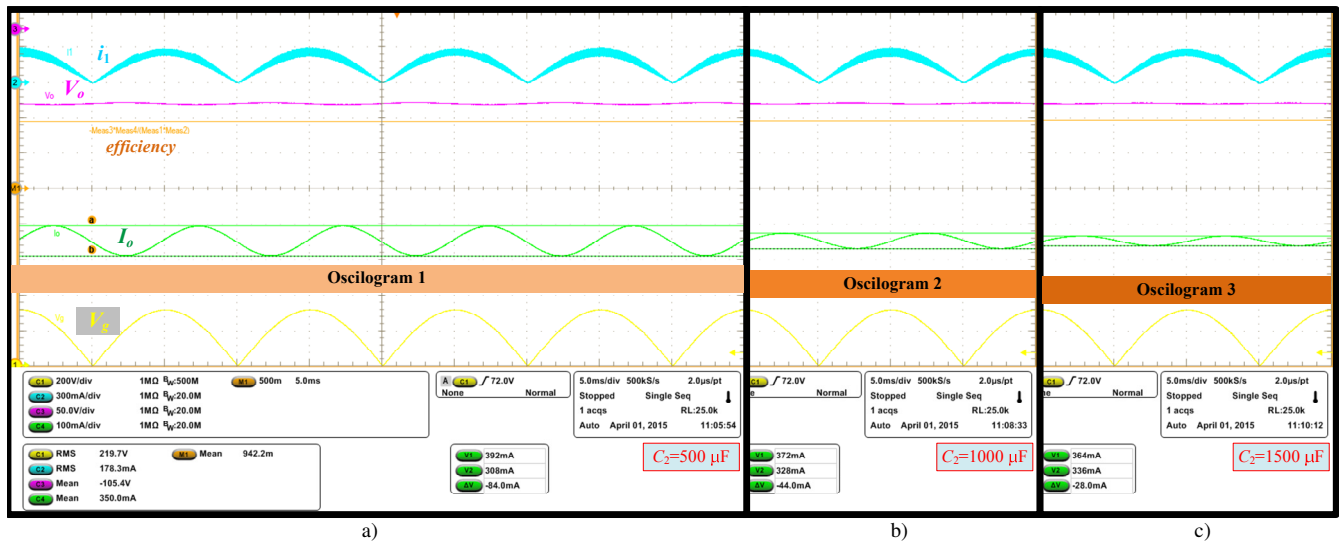


Fig. 24 Efficiency and output current ripple for different values of output capacitance a) $C_2 = 500 \mu\text{F}$, b) $C_2 = 1000 \mu\text{F}$, c) $C_2 = 1500 \mu\text{F}$.

For the purpose of comparison, the output current predicted by the SSM with or without the perturbation produced by the sinusoidal input voltage is plotted respectively as $I_{oSSM|Vg=0}$, and $I_{oSSM|Vg=V_m \sin(\omega t)}$ in the same figure, and corroborates the theoretical predictions.

The corresponding experimental results are in perfect agreement with the simulation as illustrated in Fig. 26 where it can be seen how the load current tracks the reference current I_{ref} while the input variables maintain the proportionality imposed by the LFR behaviour.

V. CONCLUSIONS

This paper has shown that the Ćuk converter is a better alternative than the SEPIC converter when designing a sliding-mode control-based loss-free resistor due to its unconditionally stable nature. It has been also illustrated that the use of a variable hysteresis width in the design of the sliding-mode internal current loop eliminates the distortion in the zero-crossings of the input current by reducing significantly the I-THD while keeping a unity PF. The analysis of the ISD has led to the design of an external control loop to regulate the output

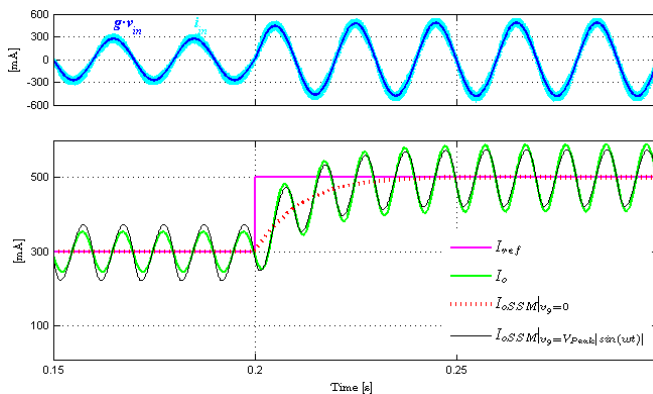


Fig. 25 Simulated output waveforms of the Ćuk converter-based LFR with output current regulation: reference current (I_{ref}), circuit output current (I_o), SSM output current ($I_{oSSM|Vg=0}$), and SSM output current considering the AC input voltage disturbances ($I_{oSSM|Vg=V_m \sin(\omega t)}$).

current supplying an HBLEDs string, which results in a wide dimmer range (from 180% to 20% of the HBLED nominal current) with a low I-THD (15%). The experimental measurements in a Ćuk converter are in good agreement with the simulations and the theoretical predictions. In comparison with the main antecedents on the use of Ćuk and SEPIC converters for HBLEDs [32-36], the work here reported presents an extensive dynamical analysis of the two controlling loops in both converters in a clear-cut contrast with the mentioned papers, which are focused on the static analysis to select the appropriate values of the passive components. A compromise among a fast output response, a small flickering and a slow value of I-THD has been solved empirically because an optimal solution for both SMC, and SMC-HM is still an open problem that could be the subject of posterior research in robust control techniques following the procedure reported in [37].

The proposed techniques in this paper can be used in the design of low power single-stage AC-DC PFC converters with a series inductor in the input port requiring a regulated variable (voltage or current) in the output port.

Prospective work contemplates an optimized design of the

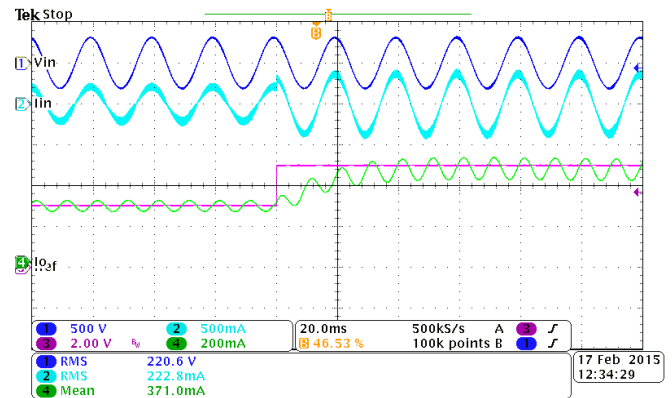


Fig. 26 Experimental waveforms of the Ćuk converter-based LFR with output current regulation: line voltage v_{in} , line current i_{in} , output current reference I_{ref} , output current I_o .

> REPLACE THIS LINE WITH YOUR PAPER IDENTIFICATION NUMBER (DOUBLE-CLICK HERE TO EDIT) < 13

controller in view of a microelectronic implementation of ASIC type.

ANNEX I

TABLE VIII SSM TRANSFER FUNCTION PARAMETERS

Cuk converter	SEPIC converter
$g_2 = 0$ $g_1 = 0$ $g_0 = r_d \cdot v_g^2 \cdot V_2$	$g_2 = r_d \cdot v_g^2 \cdot V_2 \cdot C_1 \cdot L_2$ $g_1 = 0$ $g_0 = r_d \cdot v_g^2 \cdot V_2$
$vg_1 = -r_d \cdot V_2 \cdot C_1 \cdot (V_2 + v_g)$ $vg_1 = 0$ $vg_0 = 2r_d \cdot V_2 \cdot v_g \cdot g$	$vg_2 = r_d \cdot v_g \cdot g (2V_2 + v_g) C_1 \cdot L_2$ $vg_1 = -r_d \cdot v_g \cdot C_1 \cdot V_2$ $vg_0 = 2r_d \cdot V_2 \cdot v_g \cdot g$
$rd_2 = (V_2 - V_F) V_2 \cdot C_1 \cdot L_2 (V_2 + v_g) / r_d$ $rd_1 = (V_2 - V_F) v_g^2 \cdot g \cdot L_2 / r_d$ $rd_0 = (V_2 - V_F) V_2^2 / r_d$	$rd_2 = (V_2 - V_F) V_2 \cdot C_1 \cdot L_2 (V_2 + v_g) / r_d$ $rd_1 = (V_2 - V_F) v_g^2 \cdot g \cdot L_2 / r_d$ $rd_0 = (V_2 - V_F) V_2^2 / r_d$
$vf_2 = C_1 \cdot L_2 \cdot V_2 (V_2 + v_g)$ $vf_1 = L_2 \cdot v_g^2 \cdot g$ $vf_0 = V_2^2$	$vf_2 = C_1 \cdot L_2 \cdot V_2 (V_2 + v_g)$ $vf_1 = L_2 \cdot V_2^2 \cdot g$ $vf_0 = V_2^2$
$d_3 = C_1 \cdot C_2 \cdot L_2 \cdot V_2 \cdot r_d \cdot (v_g + V_2)$ $d_2 = (C_1 \cdot V_2 (v_g + V_2) + r_d v_g^2 g C_2) L_2$ $d_1 = V_2 r_d ((C_1 + C_2) V_2 + C_1 v_g) + L_2 \cdot V_2^2 \cdot g$ $d_0 = r_d \cdot v_g^2 \cdot g + V_2^2$	$d_3 = C_1 \cdot C_2 \cdot L_2 \cdot V_2 \cdot r_d \cdot (v_g + V_2)$ $d_2 = (C_1 V_2 (v_g + V_2) + r_d v_g^2 g (C_1 + C_2)) L_2$ $d_1 = V_2^2 \cdot r_d \cdot C_2 + L_2 \cdot V_2^2 \cdot g$ $d_0 = r_d \cdot v_g^2 \cdot g + V_2^2$

REFERENCES

- [1] *Limits for Harmonic Current Emissions (Equipment Input Current ≤ 16 A Per Phase)*, IEC 61000-3-2, Part 3-2, 3rd ed., 2005.
- [2] *IEEE Recommended Practices and Requirements for Harmonic Control in Electrical Power Systems*, IEEE Std 519-1992, 1993.
- [3] H. Yuequan, L. Huber, Jovanovic, x, and M. M., "Single-Stage, Universal-Input AC/DC LED Driver With Current-Controlled Variable PFC Boost Inductor," *IEEE Transactions on Power Electronics*, vol. 27, pp. 1579-1588, 2012.
- [4] J. M. Alonso, M. A. Dalla Costa, and C. Ordiz, "Integrated Buck-Flyback Converter as a High-Power-Factor Off-Line Power Supply," *IEEE Transactions on Industrial Electronics*, vol. 55, pp. 1090-1100, 2008.
- [5] B. Singh, B. N. Singh, A. Chandra, K. Al-Haddad, A. Pandey, and D. P. Kothari, "A review of single-phase improved power quality AC-DC converters," *IEEE Transactions on Industrial Electronics*, vol. 50, pp. 962-981, 2003.
- [6] T. Qian and B. Lehman, "Buck/half-bridge input-series two-stage converter," *IET Power Electronics*, vol. 3, pp. 965-976, 2010.
- [7] A. J. Sabzali, E. H. Ismail, M. A. Al-Saffar, and A. A. Fardoun, "A new bridgeless PFC Sepic and Cuk rectifiers with low conduction and switching losses," in *IEEE International Conference on Power Electronics and Drive Systems*, 2009, pp. 550-556.
- [8] D. Gacio, J. M. Alonso, A. J. Calleja, J. Garcia, and M. Rico-Secades, "A Universal-Input Single-Stage High-Power-Factor Power Supply for HB-LEDs Based on Integrated Buck-Flyback Converter," *IEEE Transactions on Industrial Electronics*, vol. 58, pp. 589-599, 2011.
- [9] R. Erickson, M. Madigan, and S. Singer, "Design of a simple high-power-factor rectifier based on the flyback converter," in *IEEE Applied Power Electronics Conference and Exposition, APEC 1990*, pp. 792-801.
- [10] Z. Kening, Z. Jian Guo, S. Yuvarajan, and W. Da Feng, "Quasi-Active Power Factor Correction Circuit for HB LED Driver," *IEEE Transactions on Power Electronics*, vol. 23, pp. 1410-1415, 2008.
- [11] X. Xiaogao, W. Jian, Z. Chen, L. Qiang, and L. Shirong, "A Novel Output Current Estimation and Regulation Circuit for Primary Side Controlled High Power Factor Single-Stage Flyback LED Driver," *IEEE Transactions on Power Electronics*, vol. 27, pp. 4602-4612, 2012.
- [12] M. Bodelto, A. Cid-Pastor, L. Martinez-Salamero, and A. El Aroudi, "Design of an LFR based on a SEPIC converter under sliding mode control for HBLEDs applications," in *IEEE International Symposium on Circuits and Systems, ISCAS*, Rio De Janeiro, Brazil, 2011, pp. 2901-2904.
- [13] S. Singer, "Realization of loss-free resistive elements," *IEEE Transactions on Circuits and Systems*, vol. 37, pp. 54-60, 1990.
- [14] A. Cid-Pastor, L. Martinez-Salamero, A. El Aroudi, R. Giral, J. Calvente, and R. Leyva, "Synthesis of loss-free resistors based on sliding-mode control and its applications in power processing," *Control Engineering Practice*, vol. 21, pp. 689-699, 2013.
- [15] R. Haroun, A. Cid-Pastor, A. El Aroudi, and L. Martinez-Salamero, "Synthesis of Canonical Elements for Power Processing in DC Distribution Systems Using Cascaded Converters and Sliding-Mode Control," *IEEE Transactions on Power Electronics*, vol. 29, pp. 1366-1381, 2014.
- [16] A. Marcos-Pastor, E. Vidal-Idiarte, A. Cid-Pastor, and L. Martinez-Salamero, "Loss-Free Resistor-based Power Factor Correction using a Semi-bridgeless Boost Rectifier in Sliding-Mode Control," *IEEE Transactions on Power Electronics*, pp. 1-1, 2014.
- [17] M. Bodelto, A. El Aroudi, A. Cid-Pastor, J. Calvente, and L. Martinez-Salamero, "A novel control strategy to improve the power factor of a Cuk converter for HBLEDs application," in *IEEE Annual Conference of the Industrial Electronics Society, IECON*, Vienna, Austria, 2013, pp. 1950-1955.
- [18] M. Bodelto, A. El Aroudi, A. Cid-Pastor, J. Calvente, and L. Martinez-Salamero, "Sliding Mode Control of a Cuk converter with variable hysteresis width for HBLEDs applications," in *IEEE International Multi-Conference on Systems, Signals and Devices, SSD*, Castelldefels-Barcelona, Spain, 2014, pp. 1-6.
- [19] M. Bodelto, A. El Aroudi, A. Cid-Pastor, and L. Martinez-Salamero, "High performance hysteresis modulation technique for high-order PFC circuits," *Electronics Letters*, vol. 50, pp. 113-114, 2014.
- [20] V. Utkin, J. Guldner, and J. Shi, *Sliding mode control in electro-mechanical systems*, 2009.
- [21] A. Leon-Masich, H. Valderrama-Blavi, J. M. Bosque-Moncusi, J. Maixe-Altes, and L. Martinez-Salamero, "Sliding-Mode-Control-Based Boost Converter for High-Voltage-Low-Power Applications," *IEEE Transactions on Industrial Electronics*, vol. 62, pp. 229-237, 2015.
- [22] R. Haroun, A. El Aroudi, A. Cid-Pastor, G. Garica, C. Olalla, and L. Martinez-Salamero, "Impedance Matching in Photovoltaic Systems Using Cascaded Boost Converters and Sliding-Mode Control," *IEEE Transactions on Power Electronics*, vol. 30, pp. 3185-3199, 2015.
- [23] O. Lopez, L. Garcia de Vicuna, and M. Castilla, "Sliding mode control design of a boost high-power-factor pre-regulator based on the quasi-steady-state approach," in *IEEE Power Electronics Specialists Conference, PESC 2001*, pp. 932-935 vol.2.
- [24] Z. Lai and K. M. Smedley, "A family of continuous-conduction-mode power-factor-correction controllers based on the general pulse-width modulator," *IEEE Transactions on Power Electronics*, vol. 13, pp. 501-510, 1998.
- [25] M. J. Kocher and R. L. Steigerwald, "An AC-to-DC Converter with High Quality Input Waveforms," *IEEE Transactions on Industry Applications*, vol. IA-19, pp. 586-599, 1983.
- [26] J. A. Barrado, A. El Aroudi, H. Valderrama-Blavi, J. Calvente, and L. Martinez-Salamero, "Analysis of a Self-Oscillating Bidirectional DC-DC Converter in Battery Energy Storage Applications," *IEEE Transactions on Power Delivery*, vol. 27, pp. 1292-1300, 2012.
- [27] PSIM. Copyright 2001-2010 Powersim Inc. Available: <http://www.powersimtech.com>
- [28] Cree. (2013). Cree Corp.: Xlamp. Available: <http://www.cree.com/led-components-and-modules/products/xlamp/arrays-directional/xlamp-mce>
- [29] D. G. Lamar, J. Sebastian, M. Arias, and A. Fernandez, "On the Limit of the Output Capacitor Reduction in Power-Factor Correctors by Distorting the Line Input Current," *IEEE Transactions on Power Electronics*, vol. 27, pp. 1168-1176, 2012.
- [30] J. Sebastian, D. G. Lamar, M. M. Hernando, A. Rodriguez-Alonso, and A. Fernandez, "Steady-State Analysis and Modeling of Power Factor Correctors With Appreciable Voltage Ripple in the Output-Voltage

Feedback Loop to Achieve Fast Transient Response," *IEEE Transactions on Power Electronics*, vol. 24, pp. 2555-2566, 2009.

- [31] R. Erickson and D. Maksimovic, *Fundamentals of power electronics*, (2nd ed.) Kluwer Academic ed., 2001.
- [32] J. R. de Britto, A. E. Demian, L. C. de Freitas, V. J. Farias, E. A. A. Coelho, and J. B. Vieira, "A proposal of Led Lamp Driver for universal input using Ćuk converter," in *IEEE Power Electronics Specialists Conference, PESC 2008*, pp. 2640-2644.
- [33] Y. Zhongming, F. Greenfeld, and L. Zhixiang, "Single-Stage Offline SEPIC Converter with Power Factor Correction to Drive High Brightness LEDs," in *IEEE Applied Power Electronics Conference and Exposition, APEC 2009*, pp. 546-553.
- [34] Y. Zhongming, F. Greenfeld, and L. Zhixiang, "A topology study of single-phase offline AC/DC converters for high brightness white LED lighting with power factor pre-regulation and brightness dimmable," in *IEEE Annual Conference of the Industrial Electronics Society, IECON, 2008*, pp. 1961-1967.
- [35] Y. Zhongming, F. Greenfeld, and L. Zhixiang, "Offline SEPIC converter to drive the high brightness white LED for lighting applications," in *IEEE Annual Conference of the Industrial Electronics Society, IECON, 2008*, pp. 1994-2000.
- [36] Y. Zhongming, F. Greenfeld, and L. Zhixiang, "Design considerations of a high power factor SEPIC converter for high brightness white LED lighting applications," in *IEEE Power Electronics Specialists Conference, PESC 2008*, pp. 2657-2663.
- [37] O. Lopez-Santos, L. Martinez-Salamero, G. Garcia, H. Valderrama-Blavi, and T. Sierra-Polanco, "Robust Sliding-Mode Control Design for a Voltage Regulated Quadratic Boost Converter," *IEEE Transactions on Power Electronics*, vol. 30, pp. 2313-2327, 2015.



Mirko Bodetto was born in Rosario, Argentina, 1973. He graduated as an Electronics Engineer and Master in Electronics Engineering in 2010 and in 2011 respectively at the Universitat Rovira i Virgili, Tarragona, Spain. Since 2011 he is a member of the Automatic Control and Industrial Electronics Research Group (GAEI) in the same university, and the Ph.D. degree in 2015. His research interests are in the field of

power electronics applications, including dc-dc switched power supply and ac-dc power-factor-correction converters for low power applications as solid-state lighting, and renewable energy systems.



Abdelali El Aroudi was born in 1973. He received the graduate degree in Physical Science from Faculté des Sciences, Université Abdelmalek Essaadi, Tetouan, Morocco, in 1995, and the Ph.D. degree (with honors) from Universitat Politècnica de Catalunya, Barcelona, Spain in 2000. During the period 1999-2001 he was a Visiting Professor at the Department of Electronics, Electrical Engineering and Automatic Control, Technical School of Universitat Rovira i Virgili (URV), Tarragona, Spain, where he became an associate professor in 2001 and a full-time tenure Associate Professor in 2005. From September 2007 to January 2008 he was holding a visiting scholarship at the Department of Mathematics and Statistics, Universidad Nacional de Colombia, Manizales, conducting research on modeling of Power Electronics circuits for Energy Management. From February 2008 to July 2008, he was a visiting scholar at the Centre de Recherche en Sciences et Technologies de Communications et de l'Informations (CRéSTIC), Reims, France. From Sept. 2015 to Dec. 2015 he was a visiting scholar researcher LAAS-CNRS, University of Toulouse, France. From January 2015 to July 2015 he was in Petroleum Institute, Abu Dhabi, UAE as a Visiting Associate Professor where conducting research on control of power electronics switching converters for photovoltaic renewable energies applications. His research interests are in the field of structure and control of power conditioning systems for autonomous systems, power factor correction, stability problems, nonlinear phenomena, chaotic dynamics, bifurcations and control of switching converters. He has co-authored with co-workers from different universities in Europe, Asia, Africa and America more than 150 international scientific publications, 1 book and 2 book chapters. He has been involved in different national, and bilateral cooperation projects

within his research interests including the areas of control and dynamics of energy management circuits. He has given different invited lectures in Europe, Africa, Latin America and Asia.



Angel Cid-Pastor graduated as Ingeniero en Electrónica Industrial in 1999 and as Ingeniero en Automática y Electrónica Industrial in 2002 at Universitat Rovira i Virgili, Tarragona, Spain. He received the M.S. degree in design of microelectronics and microsystems circuits in 2003 from Institut National des Sciences Appliquées, Toulouse, France.

He received the Ph.D. degree from Universitat Politècnica de Catalunya, Barcelona, Spain, and from Institut National des Sciences Appliquées, LAAS-CNRS Toulouse, France in 2005 and 2006, respectively. He is currently an associated professor at the Departament d'Enginyeria Electrònica, Elèctrica i Automàtica, Escola Tècnica Superior d'Enginyeria, Universitat Rovira i Virgili, Tarragona, Spain. His research interests are in the field of power electronics and renewable energy systems.



Javier Calvente received the Ingeniero de Telecomunicación degree and the Ph.D. degree from the Universitat Politècnica de Catalunya (UPC), Barcelona, Spain, in 1994 and 2001, respectively.

He was a visiting scholar with Alcatel Space Industries, Toulouse, France, in 1998. He is currently an Associate Professor with the Departament d'Enginyeria Electrònica, Elèctrica i Automàtica, Universitat Rovira i Virgili (URV), Tarragona, Spain, where he is working in the fields of power electronics

and control systems.



Luis Martínez-Salamero received the Ingeniero de Telecomunicación degree in 1978 and the Ph.D. degree in 1984, both at the Universidad Politècnica de Catalunya, Barcelona, Spain.

From 1978 to 1992, he taught circuit theory, analog electronics and power processing at the Escuela Técnica Superior de Ingenieros de Telecomunicación de Barcelona, Barcelona, Spain. From 1992 to 1993, he was a visiting professor at the Center for Solid State Power Conditioning and Control, Department of Electrical Engineering, Duke University, Durham, NC. From 2003 to 2004 and 2010 to 2011, he was a visiting scholar at the Division of Power Devices and Power Integration of the Laboratory of Architecture and Systems Analysis (LAAS), National Agency for Scientific Research (CNRS), Toulouse, France. Since 1995 he has been a full professor with the Department of Electrical Electronic and Automatic Control Engineering, School of Electrical and Computer Engineering, Rovira i Virgili University, Tarragona, Spain, where he is the director of the Research Group in Industrial Electronics and Automatic Control (GAEI). His research interests include structure and control of power conditioning systems, namely, electrical architecture of satellites and electric vehicles, as well as nonlinear control of converters and drives, and power conditioning for renewable energy.

Dr. Martínez-Salamero has published a large number of papers in scientific journals and conference proceedings in the fields of modelling, simulation, and control of power converters, and holds a U.S. patent on dual voltage electrical distribution in vehicles. He was guest editor of the IEEE Transactions on Circuits and Systems Special Issue on Simulation, Theory and Design of Switched-Analog Networks (Aug. 1997). He organized in cooperation with the European Space Agency (ESA) the 5th European Space Power Conference (ESPC-98) in Tarragona and served during two terms (1996-2002) as a dean of the School of Electrical and Computer Engineering. He was president of Spanish Joint Chapter of the IEEE Power Electronics and Industrial Electronics Societies from 2005 to 2008, and distinguished lecturer of the IEEE Circuits and Systems Society in the period 2001-2002. He is currently distinguished professor of Rovira i Virgili University.