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- An analytical thermal resistance model for SOI and bulk FinFETs is developed.
- Self-heating has been included in a drain current model for SOI and bulk FinFETs.
- The FinFET thermal resistance model includes the role of multiple fingers and fins.

DC self-heating effects modelling in SOI and bulk FinFETs

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ABSTRACT

DC thermal effects modelling for nanometric silicon-on-insulator (SOI) and bulk fin-shaped field-effect transistors (FinFETs) is presented. Among other features, the model incorporates self-heating effects (SHEs), velocity saturation and short-channel effects. SHEs are analysed in depth by means of thermal resistances, which are determined through an equivalent thermal circuit, accounting for the degraded thermal conductivity of the ultrathin films within the device. Once the thermal resistance for single-fin devices has been validated for different gate lengths and biases, comparing the modelled output characteristics and device temperatures with numerical simulations obtained using Sentaurus Device, the thermal model is extended by circuitual analysis to multi-fin devices with multiple fingers.

Keywords: Fin-shaped field-effect transistor (FinFET), self-heating effects (SSE), thermal resistance, compact modelling.

1. Introduction

Multi-gate MOSFETs are one of the most competitive alternatives for the future scaling scenario described by Moore's law (which considers channel lengths below 20 nm), as predicted by the International Technology Roadmap for Semiconductors (ITRS) [1]. They show excellent gate controllability over the channel, leading to strong immunity to short-channel effects and an ideal sub-threshold slope [2]. In addition, random-dopant-induced variability and junction parasitic capacitances are reduced. Multi-gate devices also present high mobilities and $I_{\text{on}}/I_{\text{off}}$ ratios, which are linked to the use of undoped silicon, and the volume inversion operation connected with geometrical quantum confinement [3].

Within the multi-gate device environment, fin-shaped field-effect transistors (FinFETs, see Fig. 1(a)) show a tremendous potential for scaling, while maintaining CMOS compatibility. Both, silicon-on-insulator (SOI) and bulk based devices can be found in FinFET technology. However, a great deal of progress is still needed to effectively describe and model their thermal characteristics, due to the low thermal coupling that takes place in devices with nano-scale dimensions [4–6], which is expected to increase because of the lower thermal conductivities of the films used in prototypes for future nodes described by the ITRS.

The microelectronics community is working hard towards the development of compact models for multigate MOSFETs, particularly FinFET models [7, 8]. In this context, it is important to account for self-heating effects (SHEs) in DC and AC low-frequency regimes [9, 10], when they can even lead to negative output conductance.

Although some authors have shown a detailed thermal model accounting for the different regions of a device [5], we have chosen a local simplified scheme, accurate enough to reproduce SHEs on FinFETs [4]. In this respect, we have not deepened on non-stationary transport [11, 12] since here we are mainly focused on the thermal facet of the model (although velocity overshoot effects could have been

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incorporated in the electrical section of the model). Thus, the model we are proposing characterizes the physics of thermal conduction within the device accurately, keeping at the same time a reasonable degree of simplicity, which is an essential feature from the compact modelling viewpoint.

The structure of the SOI and bulk FinFETs under study is described in Section 2. The necessary numerical details to evaluate the proposed thermal and electric models with Sentaurus Device [13], by Synopsys, are given in Section 3, including the thermal conductivities of the ultrathin films involved in the structure. The resulting output characteristics and local channel temperatures for 3D single-fin devices are also exposed in this section. Afterwards, the single-fin FinFETs' thermal resistance is evaluated in Section 4, with the help of an equivalent thermal circuit; DC electrical and thermal modelling is also presented, as well as its numerical validation. In Section 5 the thermal model is extended by circuit analysis to multi-fin devices with multiple fins, incorporating the components associated with each element. Finally, Section 6 presents the main conclusions.

2. FinFETs under study

According to the guidelines suggested in [1], we have studied and modelled FinFETs for which the single-fin structure is shown in Fig. 1(a). Its vertical cross-section (through the gate) has been sketched in Fig. 1(b), and the corresponding geometrical parameters, taken from [1, 5] and [14–16], are listed in Table 1.

We have considered a TiN gate, whose work-function can be adjusted to 4.5 eV, showing an electrical resistivity of $270 \mu\Omega\text{cm}$ [17]. The material chosen for the high-k gate insulator is HfO_2 , which is supposed to be 3 nm thick below the lateral gates, and 20 nm deep under the top gate [18]. The silicon fin is surrounded by a SiO_2 layer, 0.8 nm thick. The two insulator films (HfO_2 and SiO_2) result in a lateral equivalent oxide thickness (EOT) of 1.3 nm. In addition, the fin height chosen is 60 nm. The fin width is set to 20 nm; for this thickness the quantum effects (of very high computational cost [19]) are known to have a lesser influence. Moreover, the source and drain extensions, 30 nm long, are covered with silicon nitride spacer dielectric [20].

An unintentional p-type 10^{15}cm^{-3} basic doping is assumed in silicon. In relation to the overlap source and drain contacts, constant n-type $5.2 \times 10^{19} \text{cm}^{-3}$ doping is present up to 24 nm into the extensions (from the border of the pads), which is the peak value of a Gaussian profile with 2.83 nm variance [16].

A typical buried oxide (BOX) layer thickness of 100 nm is chosen for SOI FinFETs. In bulk FinFETs the fin body extends down through the silicon dioxide, with the p-type 10^{15}cm^{-3} substrate doping. The resulting inactive fin (in between the active fin and the substrate) is indicated with a dotted contour in Figs. 1(a) and 1(b). Finally, a 700- μm -thick substrate is assumed [5].

3. Numerical simulation of single-fin devices

3.1. General considerations

Neither drift-diffusion nor energy transport can describe the DC I - V characteristics of transistors at nano-scale regimes, as they do not obey the thermal velocity limit on the diffusive transport of carriers across thin low-field regions [21]. However, in silicon the saturated velocity is almost the same as the thermal velocity, and therefore the drift-diffusion transport works well, particularly if accurate mobility models for this approach are employed [21–23]. In addition, this simulation scheme is more reasonable from a time-computing view, if it has to be solved self-consistently with the heat equation in 3D geometrical structures.

The impact of SHEs on the transistor performance has been analysed in depth by auto-consistently solving the heat flow equation with the Poisson and drift-diffusion equations, using Sentaurus Device [13]. The mobility model includes the degradation of the transport properties at the SiO_2 -Si interface by means of surface-roughness scattering, phonon scattering, and saturation velocity effects, through Canali and Lombardi based models; in addition, Coulomb scattering is included considering the concentration of ionized impurities (see Section 2) through the Masetti model [13]. Furthermore, the mobility model parameters have been modified for (110) wafer orientation, by reducing the low-field

mobility as in [24].

For the heat equation solution the substrate is substituted by a boundary condition, consisting of a room-temperature thermal contact located at the bottom of the structure, incorporating an equivalent surface thermal resistance, $0.023 \text{ Kcm}^2/\text{W}$, numerically evaluated to account for a thermal resistance that represent the thermal coupling of the bottom of the FinFET structure to the underlying substrate (normalized to the FinFET cross section area). Finally, the room temperature, $T_0 = 300 \text{ K}$, is set as the temperature for all metallic contacts of the devices.

3.2. Thin films thermal conductivity calculation

For a proper thermo-electrical simulation in the DC operating regime, the temperature-dependent thermal conductivity of the different layers constituting the device needs to be incorporated in the heat flow equation [23]. Furthermore, it is necessary to consider the reduction in the thermal conductivity in thin films with respect to the bulk value (by approximately one order of magnitude in the case of ultrathin films) [6, 25].

In the FinFETs under study, the gate insulators, the silicon fin, and pads are ultrathin films, therefore we have accounted for the thermal conductivity reduction explained above. For the purpose of numerical simulation within the temperature range of interest found in the usual operating regimes (between 300 K and 400 K), with data taken from [18, 20, 22] and [25–27], a general quadratic temperature dependence for all thermal conductivities (including that of thicker films), $k_{\text{film}} \approx a + bT_1 + cT_1^2$, can be used by the TCAD tool, where T_1 stands for the lattice temperature, and a , b , and c are fitting parameters for the corresponding film (see Table 2).

3.3. Output characteristics and local channel temperature

For SOI and bulk single-fin devices, the simulated output characteristics at room temperature are represented with squares (without SHEs) and triangles (with SHEs) in Figs. 2(a) and 2(b), respectively, for the two channel lengths studied: 25 nm and 50 nm. The current reduction is evident when SHEs are incorporated, due to mobility degradation. Furthermore, bulk FinFETs show a 7% higher current than their SOI counterparts, with and without SHEs. Therefore, it must be attributed to some inversion charge which is found in the oxide-semiconductor surface of the inactive fin.

On the other hand, the simulated local channel temperature, from source to drain in the intrinsic channel, has been represented in Fig. 3 with solid and dashed-dotted lines for SOI and bulk single-fin devices, respectively, where the bias chosen is $V_{\text{GS}} = V_{\text{DS}} = 1 \text{ V}$ to enhance SHEs. For both types of FinFET and for the two channel lengths under consideration, the peak temperature takes place at the end of the channel by the drain side (since the drift-diffusion scheme is being used, instead of a non-local transport approach, the peak temperature is placed less inside the drain, around 6 nm [4, 6]. This displacement does not cause a drastic variation of the thermal performance, since this characteristic is more closely linked to the resistance of the thermal paths, technologically dependent, through which the heat generated in the device operation is evacuated).

In both types of single-fin device the lattice temperature reduces, in a similar way, as the channel length increases (at around 12 K the peak values). And in bulk FinFETs, for which the current is superior, the simulated peak temperature is only 3 K lower than in their SOI counterparts, demonstrating that for single-fin devices the inactive fin role in alleviating SHEs is not decisive.

4. Single-fin thermal characterization

Several expressions for DC and AC regimes have been proposed in the literature to evaluate the thermal resistance of field-effect transistors [9]. However the I - V characteristics must be previously known, with the resulting value depending on the bias selected, or heat is assumed to flow towards the substrate. These disadvantages can be overcome when a proper equivalent thermal circuit is used [4]. The thermal circuit should correctly describe the heat flow orientation, mainly from drain to source and from the channel region to the gate, as well as maintaining a reasonable degree of simplicity, to be useful in the context of compact model development for circuit simulators.

4.1. Equivalent thermal circuit

The single-fin thermal resistance is evaluated with the equivalent thermal circuit shown in Fig. 4,

where nodes 1, 2, and 3 represent the initial, middle, and end points of the silicon channel, respectively. The contributions linked to the main device regions (from the thermal perspective) have been included by their related thermal resistances (different fractions of these thermal resistances are employed due to the symmetries found in the transistor geometrical structure), which are evaluated at room temperature.

Thus, for the silicon channel the associated longitudinal thermal resistance is R_{ch} . The extrinsic source and drain thermal resistances are R_s and R_d , respectively. The heat flux from the silicon fin to the metal gate, through both gate oxides (including top and side layers), is considered by means of R_{ox} . Different heat fluxes in the TiN gate are taken into account with R_{gt} and R_{gl} : R_{gt} models the thermal flux that spreads out laterally through the gate, and R_{gl} the heat flux contribution from the drain and source regions, through the top and side gate metals.

Inside the FinFETs, the heat is mainly produced in the channel region. In particular, the hottest spot is found at the gate-drain border, where the carriers reach **the peak temperature** (see Fig. 3). The high temperature difference expected between the drain and metal gate regions makes it necessary to incorporate a component to account for a thermal conduction path, from the drain extension towards the gate, through the nitride spacer [4]; R_{sp} denotes this component in the thermal circuit. Nevertheless, the corresponding gate to source thermal resistance can be ignored, due to the low temperature difference observed in numerical simulations between these two regions. Thus, on the source side $R_{gl}/2$ is directly connected to the border of the silicon channel (node 1 in Fig. 4).

In the case of SOI FinFETs, the back of the die has a negligible contribution to the thermal energy flow [4], [5]. However, for bulk devices the heat flow through the inactive fin towards the substrate, along the silicon body, must be considered. As Fig. 4 shows with dotted branches, the thermal resistances $R_{ch,b}$, $R_{s,b}$ and $R_{d,b}$ are incorporated in the bulk single-fin thermal circuit to account for this flow from the channel, and from the source and drain extensions. Finally, R_{sub} models the substrate thermal resistance.

The thermal components R_s , R_d , R_{ch} , R_{ox} , R_{gl} and R_{sp} are calculated as in [4]. For R_{gt} approximately the length of the resistive path is the metal gate thickness, w_{TiN} , and the cross-sectional area of the heat flux path is the average of the two areas at the sides of the interconnection, $w_{TiN} \times L$ and $h_{TiN} \times L$ in Fig. 1. Finally, for $R_{ch,b}$ the cross-sectional area of the heat flux path is that corresponding to the inactive fin region, $w_{fin} \times L$, which is $w_{fin} \times (L_{ext} + w_{pad})$ for $R_{s,b}$ and $R_{d,b}$; the length of their resistive path is the inactive fin height (*i.e.* h_{BOX}).

Thus, all thermal components, except R_{sub} , are evaluated with the expressions summarized in the appendix; R_{sub} has been determined with Sentaurus Device **through the thermal coupling of the bottom of the FinFET structure to the underlying substrate.**

4.2. Thermal resistance and device temperature modelling

In a general purpose FinFET, SHEs are modelled by evaluating the average lattice temperature in the intrinsic channels, T_l , accounting for the Joule heating produced by the device operation as follows:

$$T_l = T_o + R_{th} N_F N I_{DS} V_{ds}, \quad (1)$$

where R_{th} is the equivalent thermal resistance; N_F and N denote the number of fingers and fins (per finger), respectively; I_{DS} is the **modelled** drain current for a single-fin; $V_{ds} = V_{DS} - I_{DS} (R_{s,ohm} + R_{d,ohm})$ is the intrinsic drain to source voltage, with V_{DS} the corresponding extrinsic voltage; and $R_{s,ohm}$ and $R_{d,ohm}$ the source and drain extrinsic ohmic resistances, respectively, which are evaluated like the thermal ones, R_s and R_d , by substituting the electrical for thermal conductivities [23] (equipotential inter-finger source/drain contacts are assumed).

According to the modelled lattice temperature (1), the thermal resistance must be evaluated on average along the channels. Thus, for single-fin devices ($N_F = N = 1$) the thermal resistance, $R_{th} = R_{1,1}$, is obtained as in [22]: the average of the thermal resistances from nodes 1, 2, and 3 in the corresponding single-fin thermal circuit, to room-temperature nodes (see Fig. 4). Its value is shown in Table 3 for both types of FinFET and the two gate lengths studied. In general, $R_{1,1}$ rises as the gate length increases, and is lower for bulk FinFETs than for their SOI counterparts, but still superior to those for

the double-gate MOSFETs (DGMOSFETs) in [22], with similar channel lengths and silicon thicknesses (according to [10]). This lower thermal coupling in FinFETs between the silicon body and the outer device areas is linked to the enhanced heating confinement, with channels more surrounded by oxide layers.

On the other hand, the drain current **model used in (1)** is based on a previous DGMOSFET charge control model presented in [28]. This model works well for the FinFETs under study here, since the contribution of the inversion charge under the top gate is low in comparison with the charge associated with the side gates. Thus, the current is calculated as in [22], for all significant operating regimes, with a scheme similar to [29] for the calculation of the saturation current, inclusive of the velocity saturation and pinch-off region length. The effective mobility model is based on the model presented in [30], whose parameters are fitted with simulation data, and the result is the same for the two channel lengths studied. Then, the low-field mobility dependence used, $\mu_{\text{eff}} = \mu_{\text{eff}_0} (T_0/T_1)^{0.8}$, is close to the one described in [6] (the exponent, 0.8, is lower) and in [31] (in this case the exponent is higher) for ultrathin body SOI devices, and the velocity saturation dependence is $v_{\text{sat}} = 2.4 \times 10^7 / [1 + 0.8 \exp(T_1/600)]$ cm/s.

The extension of the active oxide-semiconductor surface in bulk FinFETs, observed in numerical simulations, is modelled using a correction in the silicon fin height ($h_{\text{fin}} \times 1.07$), which proved to work correctly in the operating regimes considered (it is not the case for the sub-threshold region, when volume inversion dominates over surface inversion and SHEs are negligible).

The device temperature and current are modelled through an iterative procedure; for each iteration T_1 is recalculated using (1), where I_{DS} is evaluated with the lattice temperature of the previous iteration, until convergence is achieved. In the case of SOI and bulk single-fin devices, the resulting modelled output characteristics at room temperature are shown with solid lines (without SHEs) and dashed lines (with SHEs) in Figs. 2(a) and 2(b), respectively. A good fit of the simulation results is achieved for the two channel lengths studied. The bulk FinFETs' fit works better for the longer device, which is expected since the uniformity of the charge in the inactive fin is altered less by short-channel effects.

Finally, the simulated local temperature along the intrinsic channel of the single-fin devices has also been successfully compared with the T_1 obtained when the model converges (hollow triangles in Fig. 3). Simulated and modelled temperatures for the same biases show similar behaviour in both types of device (as Subsection 3.3 describes), with a relative error between them lower than 3.8%.

5. Thermal characterization of multi-fin devices with multiple fingers

Once the thermal characterization of the single-fin devices has been validated, the thermal model is extended to multi-fin devices, with multiple fingers, appropriately connecting the constituting fin thermal circuits through the inter-fin gate and the inter-finger source/drain resistances. Then, applying the iterative procedure described for single-fin devices, with thermal resistances obtained by circuit analysis as follows, the device temperature of the general purpose FinFETs can be predicted.

The following scalable model for the FinFETs' thermal resistance with the number of fins, N , and fingers, N_F , can be extracted from experimental measurements in [10]:

$$\frac{1}{R_{\text{th}}} = \frac{N_F^2}{R_{1,1} + R_{\infty,1}(N_F - 1)} + \frac{N_F^2(N - 1)}{R_{1,\infty} + R_{\infty,\infty}(N_F - 1)}, \quad (2)$$

where $R_{1,\infty}$ represents the thermal resistance per fin for multi-fin devices with single finger ($R_{\text{th}} \approx R_{1,\infty}/N$); $R_{\infty,1}$ corresponds to single-fin devices with multiple fingers ($R_{\text{th}} \approx R_{\infty,1}/N_F$); and $R_{\infty,\infty}$ stands for that of multi-fin devices with multiple fingers ($R_{\text{th}} \approx R_{\infty,\infty}/N_F N$). They can be extracted by analysis of their respective equivalent thermal circuits, as Figs. 5(a), 5(b) and 5(c) show, with R_i and R_m being the inter-fin gate and inter-finger source/drain thermal resistances, respectively.

In every case, the number of fins and/or fingers is risen (fifteen is enough) until the pads are far away from the inner fins, in this case, adding more components to the device will no longer increase the peak temperature. Then, the thermal resistance of the inner fins stops rising and its value, evaluated on average along the corresponding channel, represents the required thermal resistance per fin. Table 3 shows the resulting parameters for general purpose FinFETs, assuming a fin spacing 225 nm long [4] (*i.e.* $R_i = 2.3 \times 10^6$ K/W and 1.2×10^6 K/W for $L = 25$ nm and 50 nm, respectively), and copper inter-finger source/drain contacts [5] (*i.e.* $R_m = 5.0 \times 10^5$ K/W and 5.8×10^5 K/W for $L = 25$ nm and 50 nm, respectively).

As far as we know, very few experimental data of FinFETs' thermal resistances (strongly technologically dependant) have been published in the literature, and those found are for SOI devices. Thus, for a single-finger-40-nm SOI FinFET, with ten fins, a thermal resistance of 50×10^3 K/W has been measured in [32], meanwhile our model predicts 67×10^3 K/W with 50 nm long gates. Additionally, for a 14-nm SOI FinFET with 120 fingers, and two fins per finger, 13×10^3 K/W was obtained in [10], meanwhile our model predicts 8×10^3 K/W with the gate which length is 25 nm. Finally, for 47-nm UTB MOSFETs, $R_{1,\infty} = 638 \times 10^3$ K/W is extracted from experimental measurements in [33], close to our modeled parameter with 50 nm long gates, 508×10^3 K/W. These comparisons confirm the goodness of fit of our model in describing the thermal resistance dependence on the number of fins and fingers.

Notice that $R_{1,\infty}$ and $R_{\infty,\infty}$ do not increase with gate length as $R_{1,1}$ and $R_{\infty,1}$ do, because the heat removal path through inter-fin gate contacts is less resistive. Furthermore, all of them are lower for bulk FinFETs than for their SOI counterparts, evidencing a reduced impact of SHEs in bulk devices. In Figs. 6(a) and 6(b), the left axis represents the resulting modelled thermal resistance reduction with the number of fins (for $N_f = 1$) and fingers (for $N = 30$) respectively, with solid and dashed lines for SOI and bulk devices, and the two gate lengths studied here (25 nm and 50 nm, with triangles and squares, respectively). In the former figure, as in single-fin devices, R_{th} rises as the gate length increases; however, this dependence vanishes with the number of fins, in agreement with [33]. Thus, as expected, no influence of the gate length is observed in the last figure: data for $L = 50$ nm overlap those for $L = 25$ nm. In any case, the bulk FinFETs' thermal resistance keeps being lower than in the SOI case.

In Figs. 6(a) and 6(b), the right axis shows the corresponding **modelled temperature rise (average temperature rise in channel)** for $V_{GS} = V_{DS} = 1$ V (this bias was chosen to enhance SHEs). For both types of transistor, **the modelled temperature rise diminishes** as the gate length increases. This reduction enhances as the number of fins rises, and keeps a constant behaviour with the number of fingers. Furthermore, **the modelled temperature rise increases** with the number of fins and fingers, although a saturation value shows up (for bulk devices the impact of the number of fingers is not as significant). In any case, lower temperatures are obtained for bulk devices in comparison with their SOI counterparts. In the worst SHE case considered here (*i.e.* for $N = 30$ and $N_f = 30$) the **modelled temperature** tends to 410 (390) K for SOI devices with $L = 25$ (50) nm, respectively, and 380 (363) K for their bulk counterparts. Thus, ~ 30 K lower temperatures are obtained in bulk devices, with a 12.3% higher current (for both gate lengths).

Finally, it can be pointed out that the thermal response of bulk FinFETs would tend to that of SOI FinFETs if thinner fins were used. Nevertheless, considering the Si thermal conductivity in thin films, for an identical thermal response in both technologies (*i.e.* when $k_{Si-fin} = k_{SiO_2}$) a fin body thinner than 1 nm would be required (with BOX thicknesses superior to 100 nm) [23].

6. Conclusions

Accounting for SHEs in compact models is essential to accurately describe the DC current decrement, due to the rise in device temperature, in nanometric SOI and bulk FinFETs, mainly when multi-fin devices with multiple fingers are used. For this purpose an equivalent thermal resistance was obtained by circuital analysis, representing the temperature distribution and main heat flow paths in the device, and considering the degraded thermal conductivity of the internal thin layers. The thermal resistances, lower for bulk devices, reduce with the number of fins and fingers, and are consistent with those previously reported for other SOI technologies. Furthermore, their superior values for

higher gate lengths vanish with the number of fins. On the other hand, a DC current model including SHEs, through the thermal resistances, is used to predict the average device temperatures for the different gate lengths and biases analysed. For the same bias, it is shown that the device temperature diminishes as the gate length increases, and saturates with the number of fins and fingers. With the highest electric power, the device temperature of bulk FinFETs can be 30 K lower than in the SOI case, when multiple fins and fingers are involved, keeping the current 12.3% superior. The thermal model we present could be implemented into other well-established models to be included in circuit simulators.

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Appendix

$$R_{\text{ch}} = \frac{L}{k_{\text{Si-fin}} h_{\text{fin}} w_{\text{fin}}},$$

$$R_{\text{s}} \Big|_{h_{\text{fin}}=h_{\text{pad}}} = R_{\text{d}} \Big|_{h_{\text{fin}}=h_{\text{pad}}} \approx \frac{L_{\text{ext}}}{k_{\text{Si-fin}} h_{\text{fin}} w_{\text{fin}}} + \frac{w_{\text{pad}}}{k_{\text{Si-pad}} h_{\text{fin}} (w_{\text{pad}} + w_{\text{fin}})},$$

$$R_{\text{ox}} = \frac{w_{\text{SiO}_2}}{k_{\text{SiO}_2-0.8 \text{ nm}} L (w_{\text{fin}} + 2h_{\text{fin}})} + \frac{h_{\text{HfO}_2} w_{\text{HfO}_2}}{L (k_{\text{HfO}_2-3 \text{ nm}} 2h_{\text{fin}} h_{\text{HfO}_2} + k_{\text{HfO}_2-20 \text{ nm}} w_{\text{fin}} w_{\text{HfO}_2})},$$

$$R_{\text{gt}} \approx \frac{2w_{\text{TiN}}}{k_{\text{TiN}} (h_{\text{TiN}} + w_{\text{TiN}}) L} = \frac{2w_{\text{TiN}}}{k_{\text{TiN}} (h_{\text{fin}} + w_{\text{SiO}_2} + h_{\text{HfO}_2} + 2w_{\text{TiN}}) L},$$

$$R_{\text{sp}} \approx \frac{10^{-6}}{k_{\text{SiO}_2} w_{\text{fin}} (h_{\text{fin}} + w_{\text{SiO}_2} + h_{\text{HfO}_2} + w_{\text{TiN}})},$$

$$R_{\text{gl}} = \frac{L}{k_{\text{TiN}} w_{\text{TiN}} [2(h_{\text{TiN}} + w_{\text{SiO}_2} + w_{\text{HfO}_2}) + w_{\text{fin}}]},$$

$$R_{\text{ch,b}} = \frac{h_{\text{BOX}}}{L w_{\text{fin}} k_{\text{Si-fin}}},$$

$$R_{\text{s,b}} = R_{\text{d,b}} = \frac{h_{\text{BOX}}}{(L_{\text{ext}} + w_{\text{pad}}) w_{\text{fin}} k_{\text{Si-fin}}}.$$

References

- [1] International Technology Roadmap for Semiconductors (ITRS). Available Online <www.itrs.net/reports.html>, 2011.
- [2] J. P. Colinge, FinFETs and Other Multi-Gate Transistors, Springer Verlag, New York, 2008.
- [3] F. Gámiz, J.B. Roldán, A. Godoy, J.E. Carceller, P. Cartujo, Double gate silicon on insulator transistors. A Monte Carlo study, Solid State Electron. 48 (2004) 937–945.
- [4] B. Swahn, S. Hassoun, Electro-thermal analysis of multi-fin devices, IEEE Trans. Very Large Scale Integr. (VLSI) Syst. 16 (2008) 816–829.
- [5] M. Shrivastava, M. Agrawal, S. Mahajan, H. Gossner, T. Schulz, D.K. Sharma, V.R. Rao, Physical insight toward heat transport and an improved electrothermal modeling framework for FinFET architectures, IEEE Trans. Electron Devices 59 (2012) 1353–1363.
- [6] E. Pop, S. Sinha, K.E. Goodson, Heat generation and transport in nanometer-scale transistors, Proc. IEEE 94 (2006) 1587–1601.
- [7] A. Cerdeira, I. Garduño, J. Tinoco, R. Ritzenthaler, J. Franco, M. Togo, T. Chiarella, C. Claeys, Charge based DC compact modeling of bulk FinFET transistor, Solid State Electron. 87 (2013) 11–16.
- [8] A. Yesayan, F. Pregaldiny, N. Chevillon, C. Lallement, J.M. Sallese, Physics-based compact model for ultra-scaled FinFETs, Solid State Electron. 62 (2011) 165–173.
- [9] S. Makovejev, S.H. Olsen, V. Kilchytska, J.-P. Raskin, Time and frequency domain characterization of transistor self-heating, IEEE Trans. Electron Devices 60 (2013) 1844–1851.
- [10] S. Lee, R. Wachnik, P. Hyde, L. Wagner, J. Johnson, A. Chou, A. Kumar, S. Narasimha, T. Standaert, B. Greene, T. Yamashita, J. Johnson, K. Balakrishnan, H. Bu, S. Springer, G. Freeman, W. Henson, E. Nowak, Experimental analysis and modeling of self heating effect in dielectric isolated planar and fin devices, Proc. IEEE VLSIT (2013) 248–249.
- [11] M. Aldegunde, A.J. Garcia-Loureiro, K. Kalna, 3D finite element Monte Carlo simulations of multigate nanoscale transistors, IEEE Trans. Electron Devices 60 (2013) 1561–1567.
- [12] J. Lindberg, M. Aldegunde, D. Nagy, W.G. Dettmer, K. Kalna, A.J. Garcia-Loureiro, D. Peric, Quantum corrections based on the 2D Schrodinger equation for 3D finite element Monte Carlo simulations of nanoscaled FinFETs, IEEE Trans. Electron Devices 61 (2013) 423–429.
- [13] Sentaurus Device Users' Manual, Synopsys Inc., Mountain View, CA, 2010.

- [14]M. Hinz, O. Marti, B. Gostmann, M.A. Lantz, U. Dürig, High resolution vacuum scanning thermal microscopy of HfO₂ and SiO₂, *Appl. Phys. Lett.* 92 (2008) 043122.
- [15]D. Ha, H. Takeuchi, Y.-K. Choi, T.-J. King, Molybdenum gate technology for ultrathin-body MOSFETs and FinFETs, *IEEE Trans. Electron Devices* 51 (2004) 1989–1996.
- [16]A. Nandi, A.K. Saxena, S. Dasgupta, Impact of dual-k spacer on analog performance of underlap FinFET, *Microelectron. J.* 43 (2012) 883–887.
- [17]L.P.B. Lima, J.A. Diniz, I. Doi, J.G. Fo, Titanium nitride as electrode for MOS technology and Schottky diode: Alternative extraction method of titanium nitride work function, *Microelectron. Eng.* 92 (2012) 86–90.
- [18]M.A. Panzer, M. Shandalov, J.A. Rowlette, Y. Oshima, Y.W. Chen, P.C. McIntyre, K.E. Goodson, Thermal properties of ultrathin hafnium oxide gate dielectric films, *IEEE Electron Device Lett.* 30 (2009) 1269–1271.
- [19]C. Sampedro, F. Gámiz, A. Godoy, R. Valín, A. García-Loureiro, N. Rodríguez, I.M. Tienda-Luna, F. Martinez-Carricondo, B. Biel, Multi-subband ensemble Monte Carlo simulation of bulk MOSFETs for the 32 nm-node and beyond, *Solid State Electron.* 65–66 (2011) 88–93.
- [20]M. von Arx, O. Paul, H. Baltes, Process-dependent thin-film thermal conductivities for thermal CMOS MEMS, *J. Microelectromech. Syst.* 9 (2000) 136–145.
- [21]K. Banoo, M.S. Lundstrom, Electron transport in a model Si transistor, *Solid State Electron.* 44 (2000) 1689–1695.
- [22]J.B. Roldán, B. González, B. Iñiguez, A.M. Roldán, A. Lázaro, A. Cerdeira, In-depth analysis and modelling of self-heating effects in nanometric DGMOSFETs, *Solid State Electron.* 79 (2013) 179–184.
- [23]B. González, B. Iñiguez, A. Lázaro, A. Cerdeira, Numerical dc self-heating in planar double-gate MOSFETs, *Semicond. Sci. Technol.* 26 (2011) 095014.
- [24]F. Gamiz, L. Donetti, N. Rodriguez, Anisotropy of electron mobility in arbitrarily oriented FinFETs, *Proc. IEEE ESSDERC* (2007) 378–381.
- [25]S.M. Lee, D.G. Cahill, Heat transport in thin dielectric films, *J. Appl. Phys.* 81 (1997) 2590–2595.
- [26]X. Huang, W.-C. Lee, C. Kuo, D. Hisamoto, L. Chang, J. Kedzierski, E. Anderson, H. Takeuchi, Y.-K. Choi, K. Asano, V. Subramanian, T.-J. King, J. Bokor, C. Hu, Sub 50-nm FinFET: PMOS, *IEDM Tech. Dig.* (1999) 67–70.
- [27]J.F. Shackelford, W. Alexander, *Materials Science and Engineering Handbook*, third ed., CRC Press LLC, New York, 2001.
- [28]O. Moldovan, D. Jimenez, J.R. Guitart, F.A. Chaves, B. Iñiguez, Explicit analytical charge and capacitance models of undoped double-gate MOSFETs, *IEEE Trans. Electron Devices* 54 (2007) 1718–1724.
- [29]J.B. Roldán, F. Gámiz, F. Jiménez-Molinos, C. Sampedro, A. Godoy, F.J. García, N. Rodríguez, An analytical I–V model for surrounding-gate transistors that includes quantum and velocity overshoot effects, *IEEE Trans. Electron Devices* 57 (2010) 2925–2933.
- [30]M. Cheralathan, C. Sampedro, J.B. Roldán, F. Gámiz, G. Iannaccone, E. Sangiorgi, B. Iñiguez, Compact drain-current model for reproducing advanced transport models in nanoscale double-gate MOSFETs, *Semicond. Sci. Technol.* 26 (2011) 095015.
- [31]M. Cheralathan, C. Sampedro, F. Gámiz, B. Iñiguez, Analytical drain current model using temperature dependence model in nanoscale double-gate (DG) MOSFETs, *Proc. IEEE ULIS* (2013) 141–144.
- [32]K. Ota, M. Saitoh, C. Tanaka, Y. Nakabayashi, T. Numata, Experimental study of self-heating effects in trigate nanowire MOSFETs considering device geometry, *IEEE Trans. Electron Devices* 59 (2012) 3239–3242.
- [33]S. Makovejev, S. Barraud, T. Poiroux, O. Rozeau, J.-P. Raskin, D. Flandre, V. Kilchytska, Impact of self-heating on UTB MOSFET parameters, Tenth Workshop of the Thematic Network on Silicon on Insulator Technology, Devices and Circuits – EUROSOI (2014), O14.

FIGURES

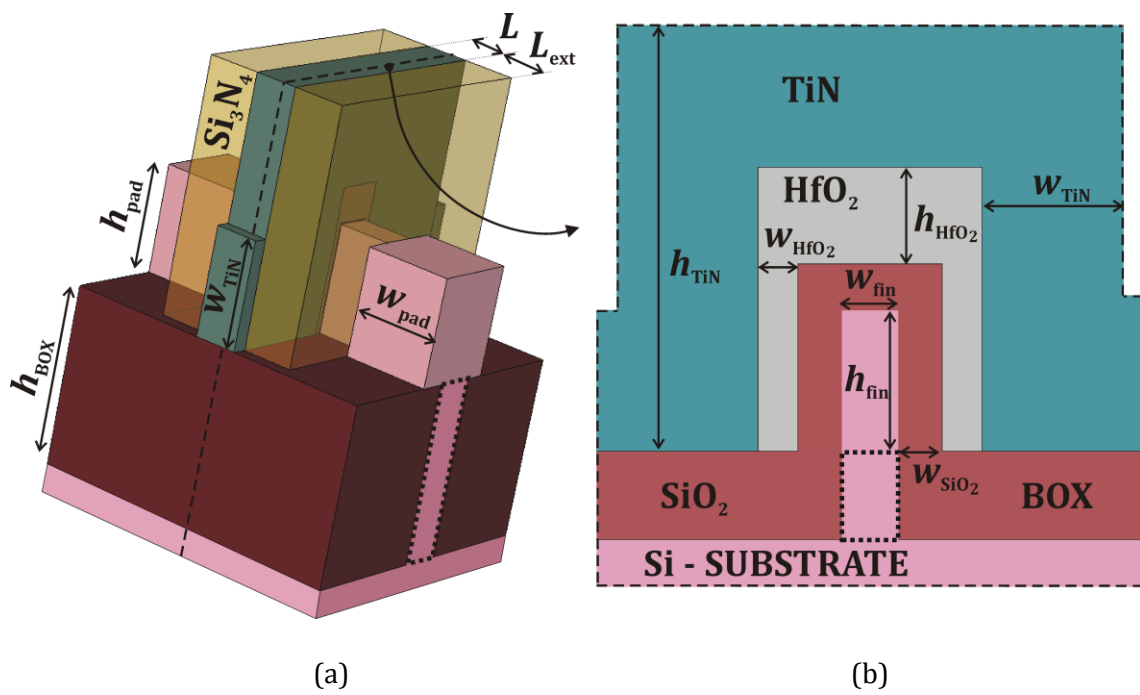
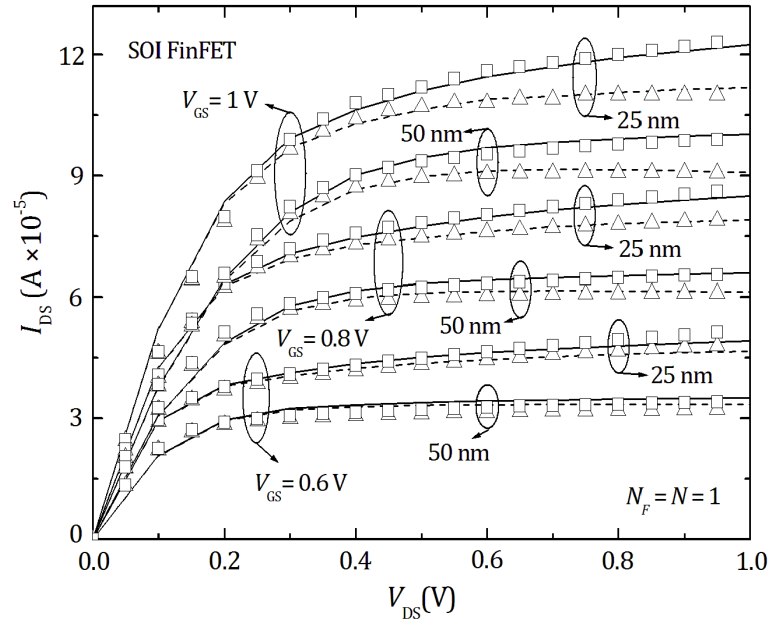
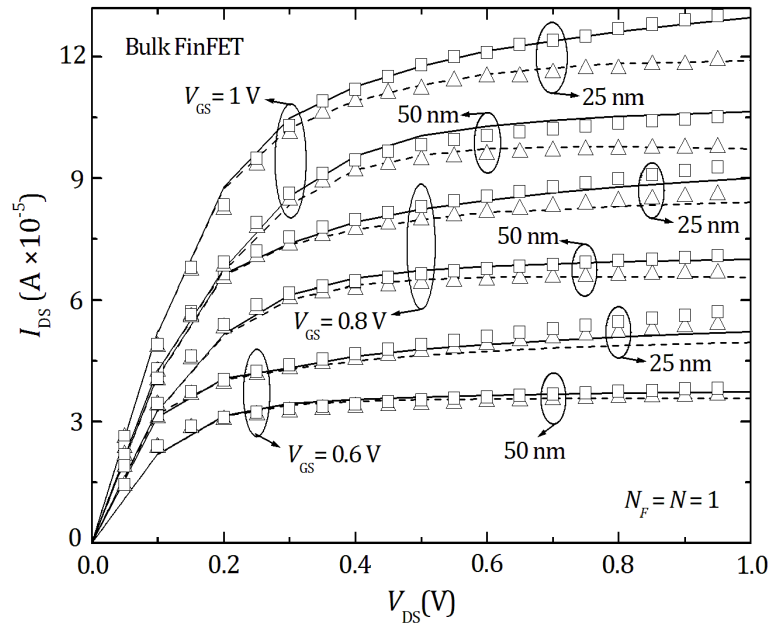


Fig. 1. (a) FinFET under study: single-fin. (b) Cross-sectional view through the gate (not drawn to scale). The inactive fin added for bulk FinFETs is indicated with a dotted contour.



(a)



(b)

Fig. 2. Output characteristics for single-fin devices with $L = 25$ nm and 50 nm, and $V_{GS} = 0.6, 0.8,$ and 1 V. Simulation results are shown as symbols (room-temperature results as squares and data including SHEs as triangles), and modelled data as lines (room-temperature results as solid lines and data including SHEs as dashed lines). (a) SOI FinFETs. (b) Bulk FinFETs.

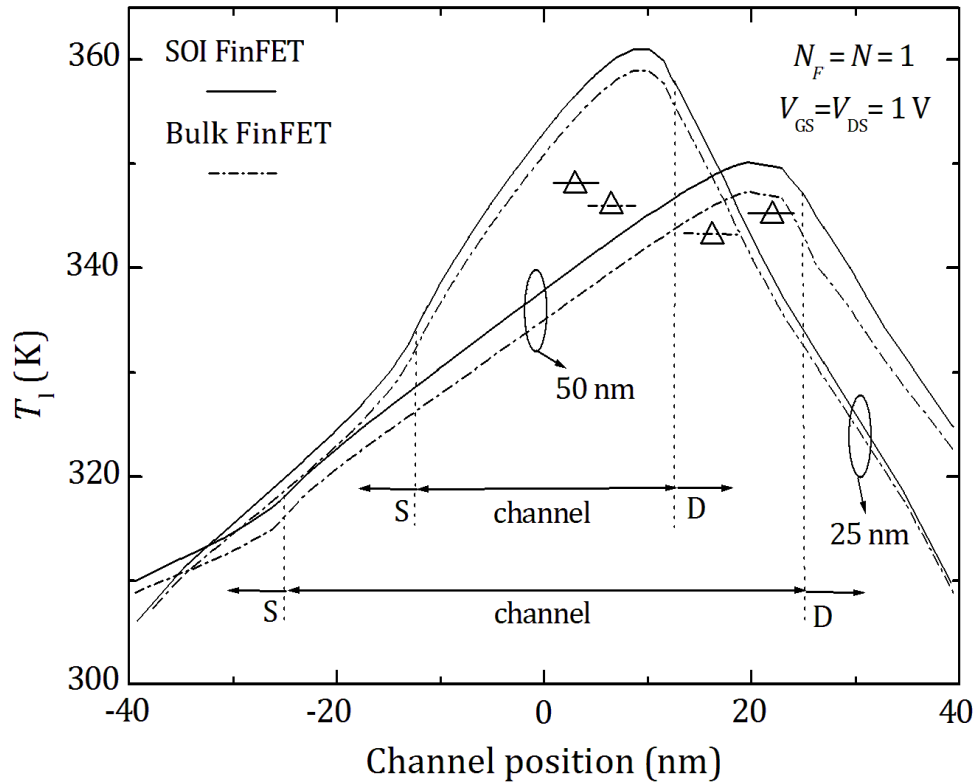


Fig. 3. Simulated local channel temperature **at the top of the fin** vs. position along the channel **(0 nm corresponds to center of the device)**, for the SOI and bulk single-fin devices, is shown as solid and dashed-dotted lines, respectively, with $L = 25$ nm and 50 nm, and $V_{GS} = V_{DS} = 1$ V. The average channel temperature obtained using the model, accounting for SHEs, is shown as hollow triangles (the corresponding horizontal line has been added to ease the comparison with the local temperature).

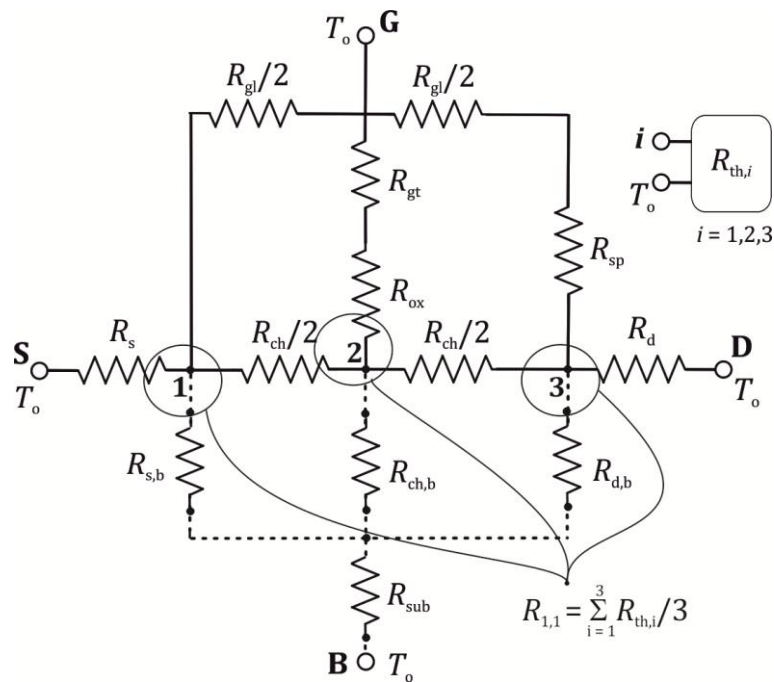


Fig. 4. Single-fin thermal circuit; dotted branches are for bulk FinFETs.

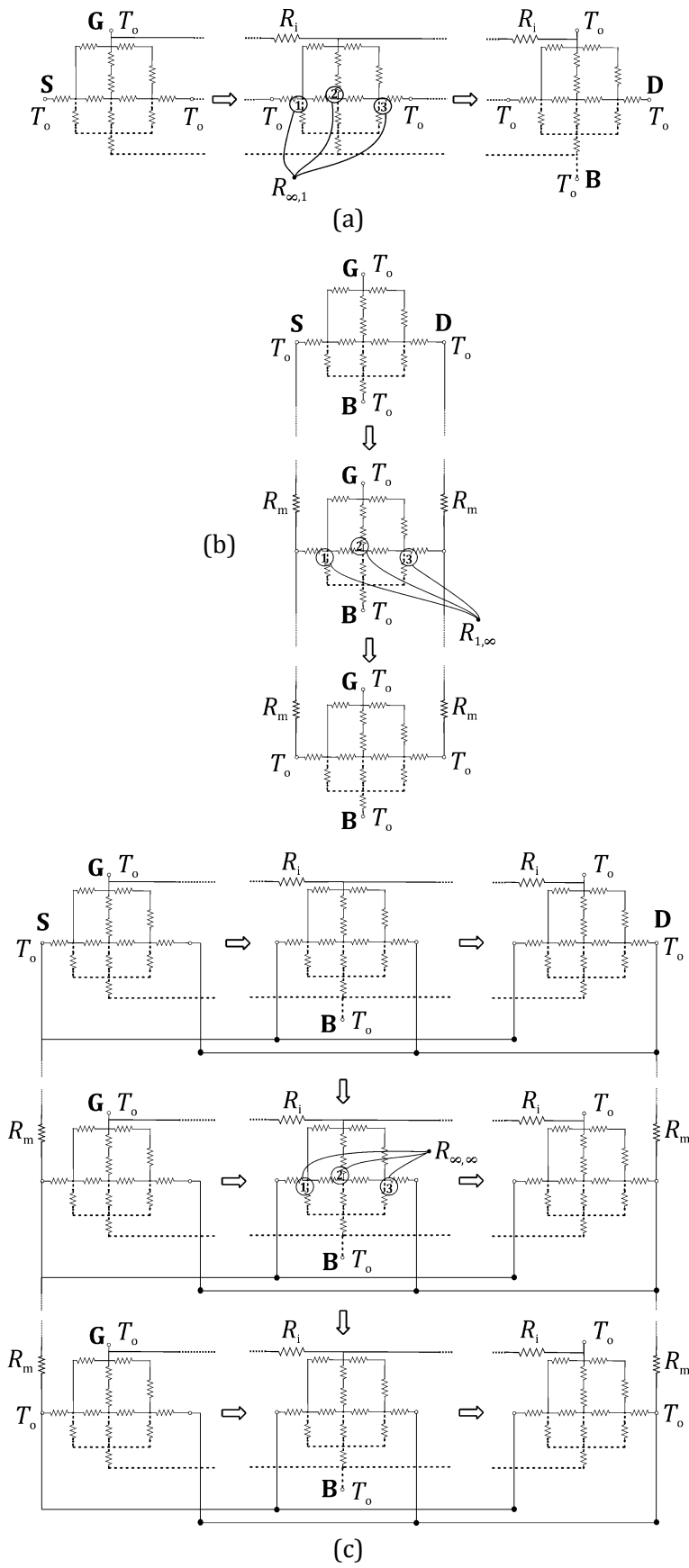
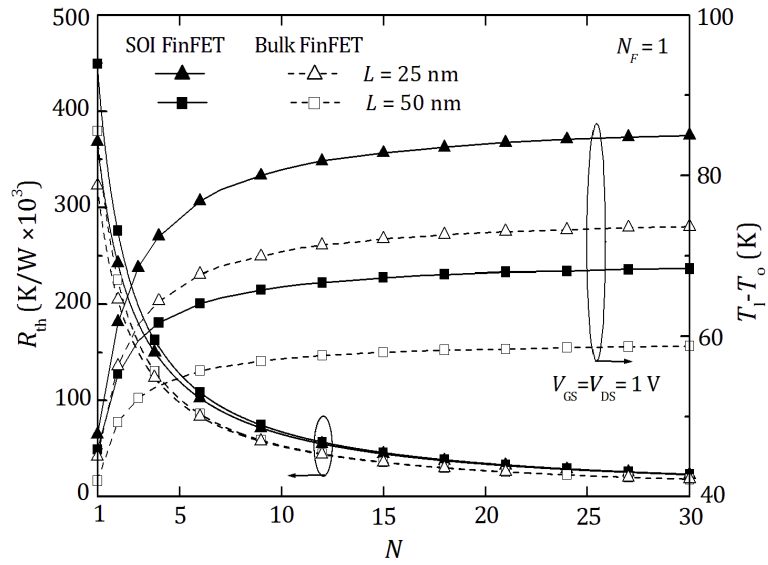
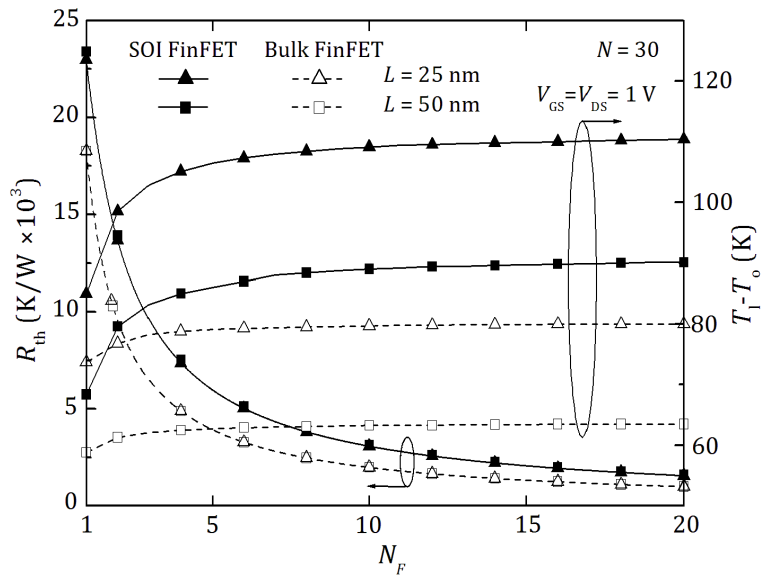


Fig. 5. Thermal circuits for: (a) Multi-fin devices with single finger ($N_F = 1, N \gg 1$). (b) Single-fin devices with multiple fingers ($N_F \gg 1, N = 1$). (c) Multi-fin devices with multiple fingers ($N_F \gg 1, N \gg 1$); dotted branches are for bulk FinFETs.



(a)



(b)

Fig. 6. Thermal resistance (left axis) and modelled temperature rise with $V_{GS} = V_{DS} = 1$ V (right axis) for SOI and bulk multi-fin devices are shown as solid and dashed lines, respectively, for $L = 25$ nm (triangles) and $L = 50$ nm (squares). (a) Versus number of fins for $N_f = 1$. (b) Versus number of fingers for $N = 30$ (in this case, R_{th} for $L = 25$ nm and 50 nm are very similar); $T_o = 300$ K.

TABLES

Table 1
FinFET geometrical parameters (nm).

$L = 25, 50$									
w_{fin}	h_{fin}	L_{ext}	w_{pad}	h_{pad}	w_{SiO_2}	w_{HfO_2}	h_{HfO_2}	w_{TiN}	h_{BOX}
20	60	30	50	60	0.8	3	20	60	100

Table 2
Thermal conductivity fitting parameters for films constituting the FinFETs.

Film	a	b	c
	(W/K-cm $\times 10^{-3}$)	(W/K ² -cm $\times 10^{-5}$)	(W/K ³ -cm $\times 10^{-8}$)
Si-fin-20 nm	279	-30	-
Si-pad-50 nm	704	-82	-
SiO ₂ -0.8 nm	-5.6	4.2	-4.9
SiO ₂	14	-	-
HfO ₂ -3 nm	-2.7	2.5	-2.4
HfO ₂ -20 nm	8.1	-	-
Si ₃ N ₄	4.1	9.3	-11
TiN	106	143	-276

Table 3
FinFETs' thermal resistance parameters (K/W $\times 10^3$).

L (nm)	SOI		Bulk	
	25	50	25	50
$R_{1,1}$	368	449	323	379
$R_{1,\infty}$	711	715	562	556
$R_{\infty,1}$	410	508	351	415
$R_{\infty,\infty}$	910	917	608	593

RESPONSE TO THE REVIEWER

Ms. Ref. No.: MEJ-D-14-00119

Title: DC self-heating effects modelling in SOI and bulk FinFETs
Microelectronics Journal

Changes in the manuscript are highlighted in green for the first reviewer, red for the second reviewer, and blue for both of them.

Editor/Reviewer comments:

Reviewer #1: In this submission, modeling of DC self-heating effects is presented for SOI and bulk FinFET technologies. The presentation of the paper is good. Some critical information are however missing. Authors are requested to address the following issues.

1. What is the thickness native gate-oxide? How thick HfO₂ is? What is the source / drain extension length? What fin height is assumed in this study?

We have given the thickness of HfO₂ and SiO₂ layers, the source and drain extensions and the fin height in Table 1. However, as pointing out by the referee, it is also interesting to repeat this information in Section 2 to ease the reading of the manuscript. We have done so in the new version of the manuscript.

2. Saturation on-current of ultra-scaled transistors do not follow the semi-classical drift-diffusion transport model as reported following papers. The transport models are therefore required to calibrate according to the measurement result. Any attempt to calibrate the semi-classical models has not done in this study. The study therefore may not satisfactorily describe the self-heating effect of ultra-scaled transistors. Which TCAD model is used to predict self-heating effects in this study?

[a] R A Kranti and G A Armstrong, "SRAM cell design with nanoscale double-gate SOI MOSFETs: impact of source/drain engineering and circuit topology," *Semiconductor Science and Technology* 2008

[b] M. Aldegunde et al., "3D finite element Monte Carlo simulations of multigate nanoscale transistors," *IEEE TED*, May 2013.

[c] J. Lindberg et al., "Quantum corrections based on the 2D Schrodinger equation for 3D finite element Monte Carlo simulations of nanoscaled FinFETs," *IEEE TED*, Feb. 2014.

The referee is right at pointing out the need of other transport approaches to reproduce the transport at the drain side in these nanometric devices. Nevertheless, our modeling efforts (the main purpose of this paper is linked to model development) are devoted to the thermal effects. We could have included non-local transport effects (non-stationary transport effects), such as velocity overshoot, in our compact model to account for this transport regime (see refs. 29 and 30 in the manuscript to see previous implementations). In this respect, by combining a model including

velocity overshoot with the thermal model we are presenting here, we could reproduce the main physical mechanisms involved in the device operation. Nevertheless, we believe that the thermal model (the new addition here) is accurate enough to reproduce the thermal effects of the device, even if non-stationary transport effects are considered. In this respect, the thermal model might be more accurate if other terms are included (within the thermal model), but from the compact modeling viewpoint it is not worth complicating the model implementation, since the simulation of circuits with thousands of components would not be feasible. This is clarified in Section 1, where the suggested reviewer's references ([b] and [c]) have been also incorporated.

For the electron mobility in Sentaurus Device, Canali, Masetti and Lombardi based models are being used, as indicated in text, Subsection 3.1.

3. What is surface thermal resistance? How you determine the value of surface thermal resistance?

In line with the simplification approach followed in the thermal model development to deal with the tradeoff, we have always to face when dealing with compact models (simplicity and accuracy), we have not considered specifically surface thermal resistances. However, the effects of these resistances in the different parts of the device could be merged (and tuned later on) with the already existing components of the thermal model, which are representative enough to model the main thermal circuits within the device. See the degree of accuracy obtained with the model (Figure 2) taking into consideration the complexity of the device geometry.

In addition, the surface thermal resistance commented in Subsection 3.1 represents the equivalent substrate thermal resistance, assuming a representative Si substrate of dimensions $0.7 \times 1 \times 1 \text{ mm}^3$ (this calculation was performed for simplification purposes). It was estimated, from numerical simulations, to account for a thermal resistance that represent the thermal coupling of the bottom of the FinFET structure to the underlying substrate, and normalized to the FinFET cross section area. This is clarified in Subsection 3.1.

4. How the thermal conductivity calculation is integrated with device simulation? Are the values of Kfilm measured prior to the simulation run or it has been calculated during the simulation by the TCAD tool?

We have calculated the thermal conductivity previously; taking into account the thickness of the layers we have included in the devices simulated. As stated in the paper, we have employed published experimental data to do so. Once these data are known we have introduced them in the TCAD tool, which is clarified in Subsection 3.2.

5. 20nm fin thickness is in reality too thick for a 25nm gate length device (according to the ITRS projections). Since the fin is very thick in this study, the bulk FinFETs exhibit better results as compared to the SOI FinFET. However, with appropriate fin thickness, bulk and SOI FinFET behave in similar way.

We considered many device geometries, within the ITRS projections and also previously published literature. In fact, most of the geometrical choices employed here were justified by carefully studying publications where these devices were designed, fabricated and characterized (see explanations given in Section 2). In this respect,

we believe that the devices employed are representative enough for model development; in this context is where we are making use of them. However, as the referee indicates, the thinner the fin is, the thermal response of bulk FinFETs is closer to that of SOI FinFETs. Nevertheless, considering the Si thermal conductivity in thin films, for an identical thermal response in both technologies a fin body thinner than 1 nm would be required (with BOX thicknesses superior to 100 nm). This is pointed out at the end of Section 5.

6. What is the bulk doping concentration in bulk FinFET? Bulk doping will cause additional scattering in the channel region. It is not clear whether it has been addressed in the simulation.

We have employed conventional undoped Si (assuming 10^{15} cm^{-3} doping impurities). The effects of Coulomb scattering (this scattering mechanisms includes the effects of doping impurities addressed by the referee) are taken into consideration by modifying the corresponding Sentaurus mobility model. So in this respect, the effects are taken into account. Following the reviewer suggestion, we have clarified this issue in the text, Section 2, which is referenced in Subsection 3.1.

7. Why the peak device temperature takes place at the channel drain interface? Why it does not take place deep inside the drain?

The temperature peak takes place inside the drain (we considered gate overlap in our devices). Since the Gaussian doping distribution employed for the drain gradually decreases below the gate, the border of the drain-channel junction is not clearly defined, although it is found under the gate oxide. In this respect, the temperature peak would be within the drain or at least very close to the drain boundary.

We, nevertheless, highlight that since the drift-diffusion scheme is being used, this temperature peak would be placed less inside the drain than if a non-local transport approach were considered (Monte Carlo simulations or energy balance equations). However, we believe that the peak temperature displacement would not cause a drastic variation of the thermal performance since this characteristic is more closely linked to the resistance of the thermal paths (technologically dependent), through which the heat generated in the device operation is evacuated. This is pointed out in Subsection 3.3.

8. Why the carrier energy is maximum at channel drain interface? Is this due to the sharp change in electrical potential?

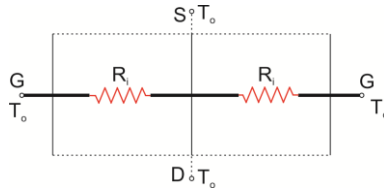
The answer to this issue is linked to the response given in the previous referee's comment. The energy distribution is also dependant on the transport approach, and for the drift-diffusion scheme of this paper it is supposed to be more on the channel side. We also believe that this effect does not affect the device thermal behaviour.

In any case, in order to avoid misunderstanding, "an energy peak" has been substituted by "the peak temperature" in Subsection 4.1.

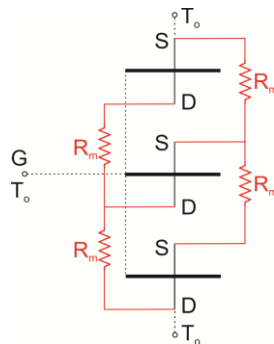
9. What is the difference between multiple fingers single fin device and multiple fin single finger device?

Temperature of external metallizations to access the device is supposed to be the room value ($T_0 = 300 \text{ K}$).

In multiple-fin-single-finger devices, a continuous material (TiN) forms the elemental gates. Therefore, T_o must be set only at the elemental gates at the final edges, and an inter-fin gate thermal resistance, R_i , is considered. The elemental sources and drains are aligned. Thus, T_o is established for them.



In multiple-finger-single-fin devices, all gates are externally accessed at room temperature. Source and drain could be misaligned; in this case an inter-finger source/drain thermal resistance, R_m , is considered, and T_o is only set at the final edges of the series of elemental sources and drains.



Therefore, multiple-fingers-single-fin and multiple-fin-single-finger devices differ on the geometrical distribution of elemental transistors, and their different thermal response depends solely on the difference of thermal resistance linked to the interconnections (figures 5(a) and 5(b) in manuscript).

10. In order to model device temperature and current, an iterative scheme has been used in this study. Is this iteration performed using TCAD tool or iteration is separately done? If the iteration is performed with TCAD tool, how do you integrate the T1 in the simulation?

No TCAD tool is employed for this. The model is implemented with a simple code developed by us, in line with a compact modeling approach. The model calculations are much faster than the Sentaurus simulations, as it should be in a compact modeling context. This is clarified in Subsection 4.2.

Reviewer #2: This paper presents a single and multi-fin thermal model for SOI and bulk finFETs extending previous work. The following comments are intended to help improve the paper.

1. In the last paragraph of section 3.3, figure 3 is discussed. It is hard to determine the reference locations for the figure; the only location indicated was the circles for the gate boarder on the drain side. Describing how the channel position relates to figure 1 would be beneficial; is a channel position of 0nm the center of the device? Also where the temperature is measured in terms of physical location would help understand the figure (center, top, bottom, etc.).

Following referee's comment, figure 3 has been modified. The physical center of the devices and the temperature locations have been clarified in the caption. The first paragraph of Section 3.3 has been also modified.

2. In section 4.1, the authors mention that R_{sub} is determined by Sentaurus Device; can any additional details be provided? For example, how does R_{sub} compare to the other thermal resistances ($R_{ch,b}$, $R_{s,b}$, or $R_{d,b}$). What are the properties of the substrate that require Sentaurus Device that make the first order L/kA type of calculation inadequate?

Surface thermal resistance, in Subsection 3.1, represents the equivalent substrate thermal resistance assuming a representative Si substrate of dimensions $0.7 \times 1 \times 1 \text{ mm}^3$. It was estimated, from numerical simulations, to account for a thermal resistance that represent the thermal coupling of the bottom of the FinFET structure to the underlying substrate, R_{sub} , which is normalized to the FinFET cross section area. This is clarified in Subsections 3.1 and 4.1. The other resistances ($R_{ch,b}$, $R_{s,b}$, or $R_{d,b}$) are different since they model different sections of the device (in order to assess the thermal resistance of the main paths that can evacuate the heat generated by means of Joule heating).

We have employed the first order L/kA approximation in the construction of the thermal model in some cases; however, the complex geometries (different materials and geometries) within the device make necessary certain approximations to simplify the modelling.

3. In section 4.2 the authors discuss finding $R_{th} = R_{1,1}$ which is the average of the thermal resistances from nodes 1, 2, and 3. However what is missing is how to calculate $R_{th,i}$ in figure 4; what is done with nodes G, D, S, and B? Are they shorted together in the resistance calculation and used as a reference? Essentially if you have an Ohm meter, how is the circuit in figure 3 configured to measure the resistance $R_{th,i}$ in each case for nodes 1, 2, and 3?

Nodes G, D, S, and B are shorted together for the thermal resistance calculation, and used as a reference. Figure 4 has been modified to clarify the procedure of the thermal resistance evaluation.

4. In section 4.2 the solution procedure mentions using an iterative method where T_1 and IDS are calculated independently, is this process used to solve (1), or is a real MOSFET model used when calculating IDS ? If a real MOSFET model is used, can you provide details on the model?

As the referee suggests, we employ an iterative method to solve Equation 1. For that purpose, we use a real MOSFET model for IDS. Once convergence is achieved we assumed that the device average temperature and current are determined.

The details of the model (the electrical part) are given in reference 22 of the paper. For the sake of clarity we have not included them here, since we were mainly focusing on the thermal facet of the model.

5. In section 5, first sentence of second paragraph mentions NF, however it appears N_F (N with subscript F) is used in (2) and below. The subscripts should be made consistent.

It has been corrected in all the manuscript.

6. Section 5, last paragraph the authors mention "For both types of transistor, the modelled temperature diminishes as the gate length increases". What is meant by "temperature diminishing"? Is this supposed to mean the temperature rise diminishes?

It means "The temperature rise diminishes". It has been corrected.

7. Figure 6, where is the temperature taken in the device? Do the figures show the maximum temperatures, average temperatures, etc? Provide clarity. Also consider mentioning the reference temperature in the figure caption; alternatively show the showing the temperature delta could improve the presentation.

Figure 6 represents the modelled temperature. That is, the average temperature in channel (we suppose a homogeneous temperature in the channel for modelling purposes, as it is conventionally done). It has been clarified in text, Section 5, following the referee's recommendation, and also temperature rises are now represented in figure 6, with the reference temperature being indicated in the figure caption.